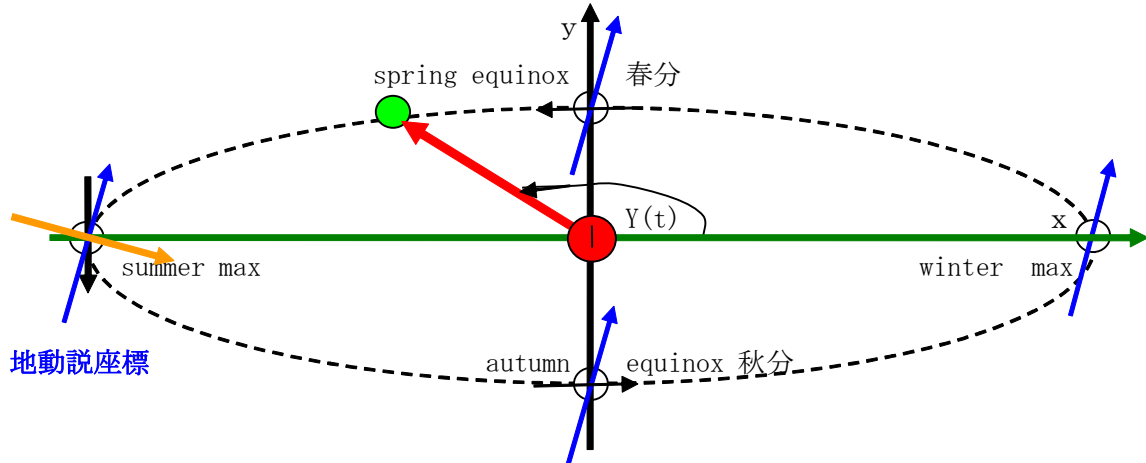


–Insolation Function(latitude Θ ; longitude ϕ , dairy angle ϕ , seasonal angle Y)–

Can you imagine north pole($\Theta=90$) is hotter than equator($\Theta=0$) at a season?.

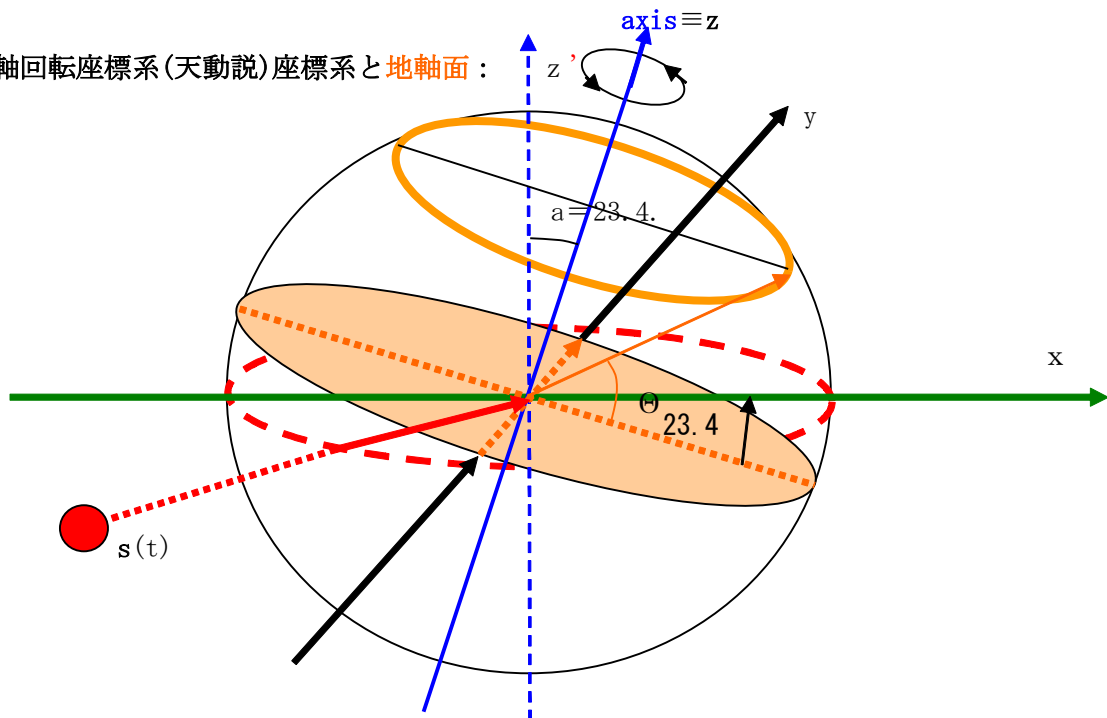
(1)year(seasonal) angle : $Y=360t/365$. $\langle 0 \leq t \leq 365 \rangle$. '09/6/13, 22, 7/6.

Geocentric theory coordinate system(x, y, z) with plane of sun orbit.



(2)geo-axial rotation(geocentric)coordinate system and(geo-axial plane):

地軸回轉座標系(天動説)座標系と地軸面:



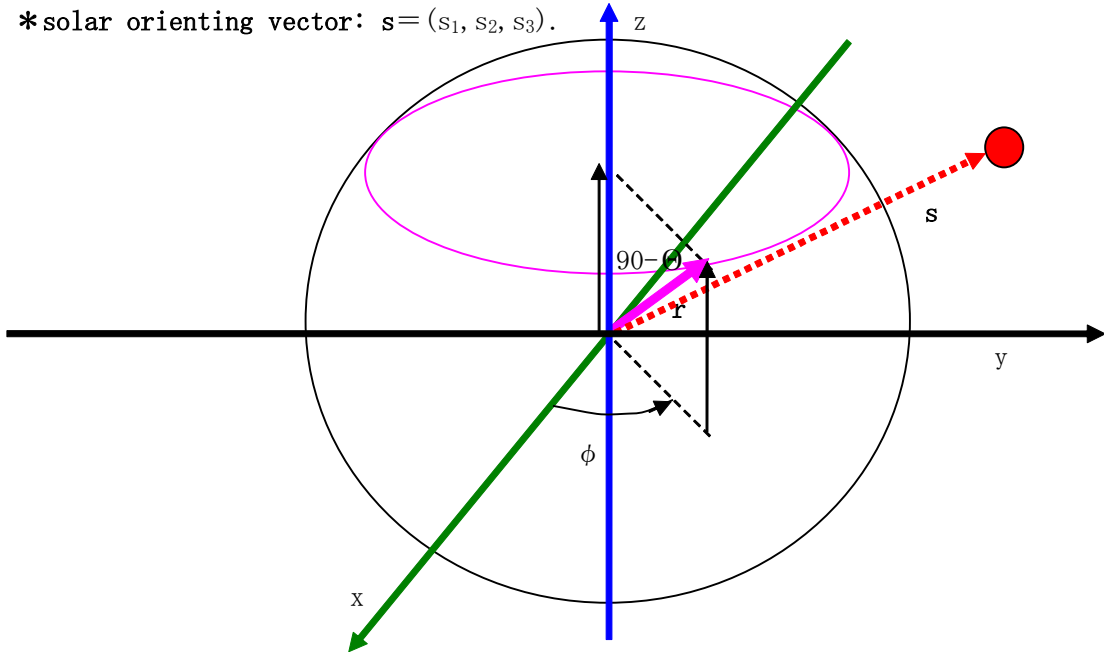
geo-axial plane plane vector $\equiv z$ axis $\equiv z$, solar orienting vector $\equiv s(t)$.

Their inner product relate with seasonal input angle χ ($Y(t)$) of insolation.

(3) Insolation dependency on angles : $\mathcal{R} = \{(\mathbf{r} \cdot \mathbf{s}) + |(\mathbf{r} \cdot \mathbf{s})|\} / 2 \geq 0$.

*position vector on earth: $\mathbf{r} = (\sin\langle 90-\Theta \rangle \cos \phi, \sin\langle 90-\Theta \rangle \sin \phi, \cos\langle 90-\Theta \rangle)$.

*solar orienting vector: $\mathbf{s} = (s_1, s_2, s_3)$.



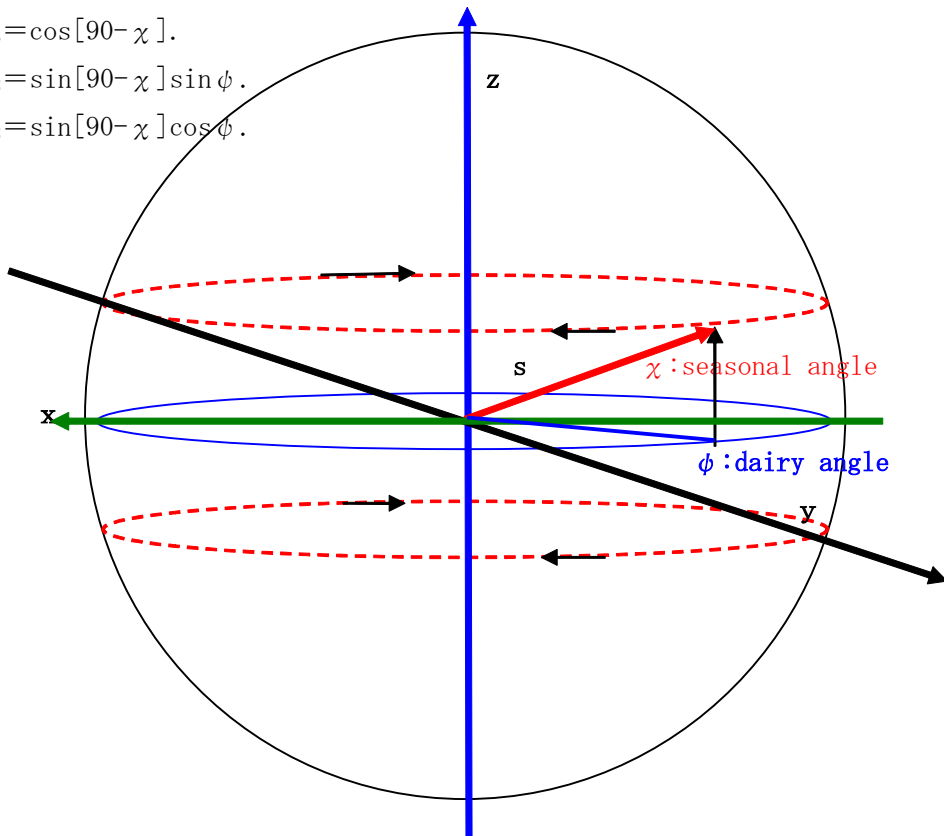
(4) solar orienting vector : $\mathbf{s} = (s_1, s_2, s_3)$ in geocentric coordinate.

$\chi = \chi(Y)$. \rightarrow seasonal angle of insolation

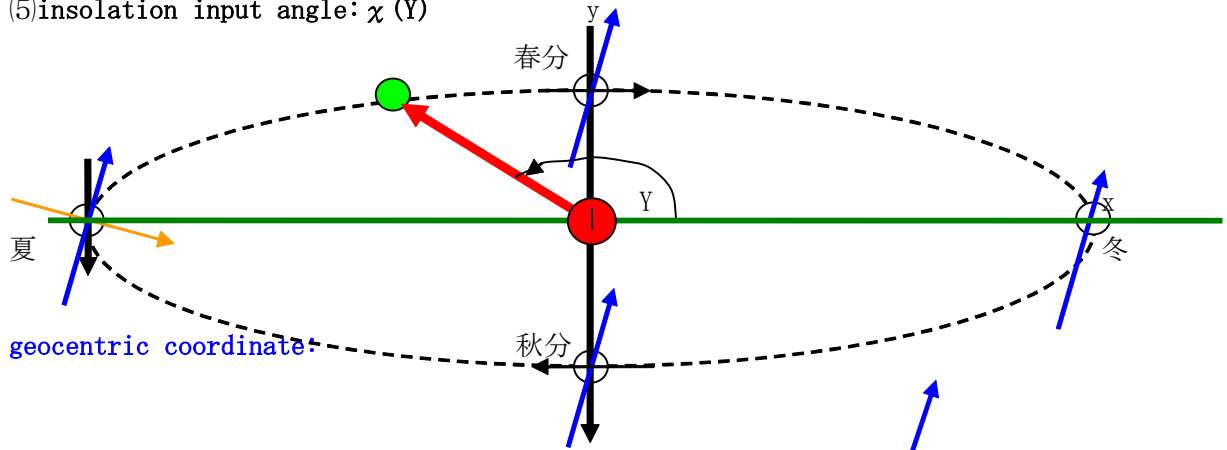
$$s_3 = \cos[90 - \chi].$$

$$s_2 = \sin[90 - \chi] \sin \phi.$$

$$s_1 = \sin[90 - \chi] \cos \phi.$$



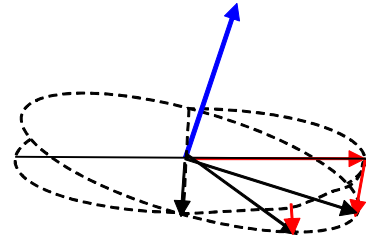
(5) insolation input angle: $\chi(Y)$



axis : $\mathbf{z} = (\sin(23.4), 0, \cos(23.4))$;

red : $\mathbf{s} = (-\cos Y, -\sin Y, 0)$.

$\langle \mathbf{z}, \mathbf{s} \rangle = \sin \chi = -\sin(23.4) \cos Y$. $Y = 360t/365$.



$$\chi(t) = -\text{Sin}^{-1} \langle \sin(23.4) \cos(360t/365) \rangle. \quad ; \text{degree.}$$

$$\chi(t) = -\text{Sin}^{-1}(\sin(0.408) \cos(2\pi t/365)). \quad ; \text{radian.}$$

(6) Insolation function $\mathcal{R}(t, x; \phi - \phi)$ as the inner product :

$$\mathbf{r} = (\sin \langle 90 - \Theta \rangle \cos \phi, \sin \langle 90 - \Theta \rangle \sin \phi, \cos \langle 90 - \Theta \rangle).$$

$$\mathbf{s} = (\sin[90 - \chi(t)] \cos \phi(t), \sin[90 - \chi(t)] \sin \phi(t), \cos[90 - \chi(t)]).$$

$$|(\mathbf{r} \cdot \mathbf{s})| = \sqrt{\langle (\mathbf{r} \cdot \mathbf{s})^2 \rangle}. \rightarrow \mathcal{R} = \{(\mathbf{r} \cdot \mathbf{s}) + |(\mathbf{r} \cdot \mathbf{s})|\} / 2.$$

$$(\mathbf{r} \cdot \mathbf{s}) = \sin[90 - \chi(t)] \sin \langle 90 - \Theta \rangle \cos \phi(t) \cos \phi$$

$$+ \sin[90 - \chi(t)] \sin \langle 90 - \Theta \rangle \sin \phi(t) \sin \phi + \cos[90 - \chi(t)] \cos \langle 90 - \Theta \rangle$$

$$= \langle \sin[90 - \chi(t)] \sin \langle 90 - \Theta \rangle \langle \cos \phi(t) \cos \phi + \sin \phi(t) \sin \phi \rangle$$

$$+ \cos[90 - \chi(t)] \cos \langle 90 - \Theta \rangle$$

$$* \quad \mathcal{R} \equiv (\mathbf{r} \cdot \mathbf{s}) = \sin[\pi/2 - \chi(t)] \sin \langle \pi/2 - \Theta \rangle \cos[\phi - \phi(t)] + \cos[\pi/2 - \chi(t)] \cos \langle \pi/2 - \Theta \rangle.$$

$$* \quad \chi(t) = -\text{Sin}^{-1}(\sin(0.408) \cos(2\pi t/365)).$$

Insolation Function {t=365days ; latitude= Θ //longitude= ϕ ;

the seasonal input angle of $\chi(t)$; dairy angle of $\phi(t)$ }:

☞ : caution : The negative value of R must be zero in $\mathcal{R} = \{(\mathbf{r} \cdot \mathbf{s}) + |(\mathbf{r} \cdot \mathbf{s})|\} / 2 \geq 0$.

\mathcal{R} is the actual function of insolation, but R is incomplete one.

(a) **Equator** : $\Theta = 0$.

$$R = (\mathbf{r} \cdot \mathbf{s}) = \sin[90 - \chi(t)] \langle \int_{-\pi/2}^{\pi/2} dt \cos[\phi - \phi(t)] / 2\pi \rangle = \sin[90 - \chi(t)] / \pi$$

24h dependency/time average

0.318(max) $\geq R(t) \geq$ 0.292(mini).

(b) **North Pole** : $\Theta = 90$.

$$R = (\mathbf{r} \cdot \mathbf{s}) = \cos[90 - \chi(t)]. \quad \chi = -\text{Sin}^{-1} \langle \sin(23.4) \cos(360t/365) \rangle > 0. \quad \text{night sun days}(t=0 \sim 182.5 \text{ 日})$$

0.397(max) $\geq R(t) \geq$ 0.

☞: surprising for us amateurs:

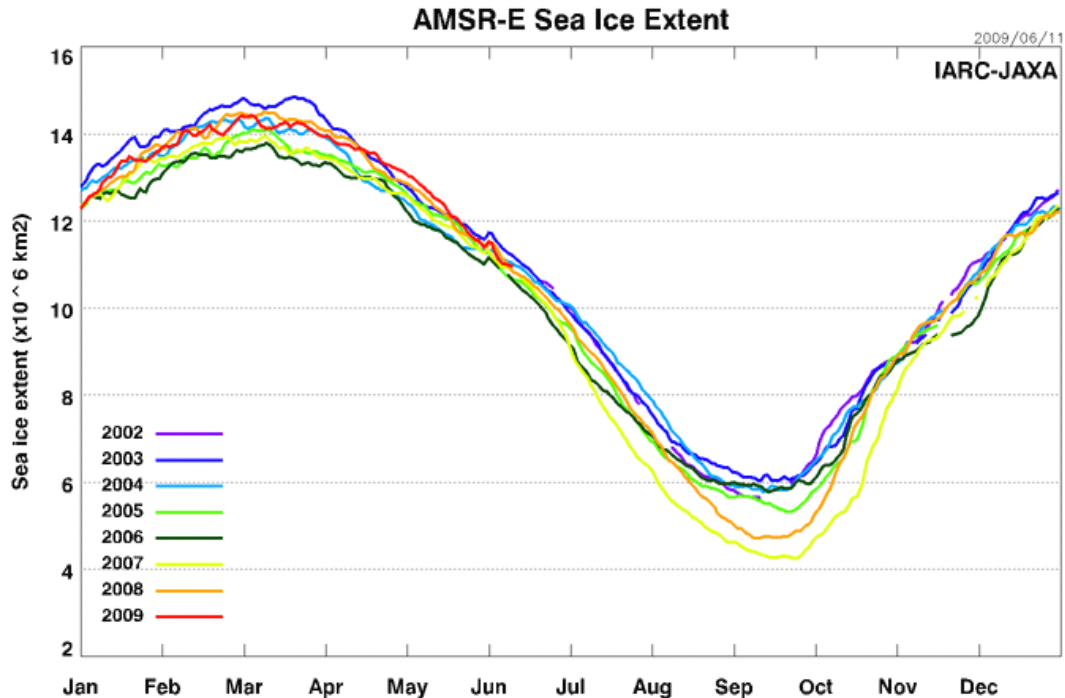
「NP is hotter than Euator in midnight sun days in 24hours total」.

Consequently 2/3 of Arctic ice cover extent can be melted in summer season.

(7) Arctic ice cover extent change in season and years:

<http://www.ijis.iarc.uaf.edu/jp/seaice/extent.Htm>

Seasonally it oscilate as alternate current componet, while the average direct current component become lower in years trend.



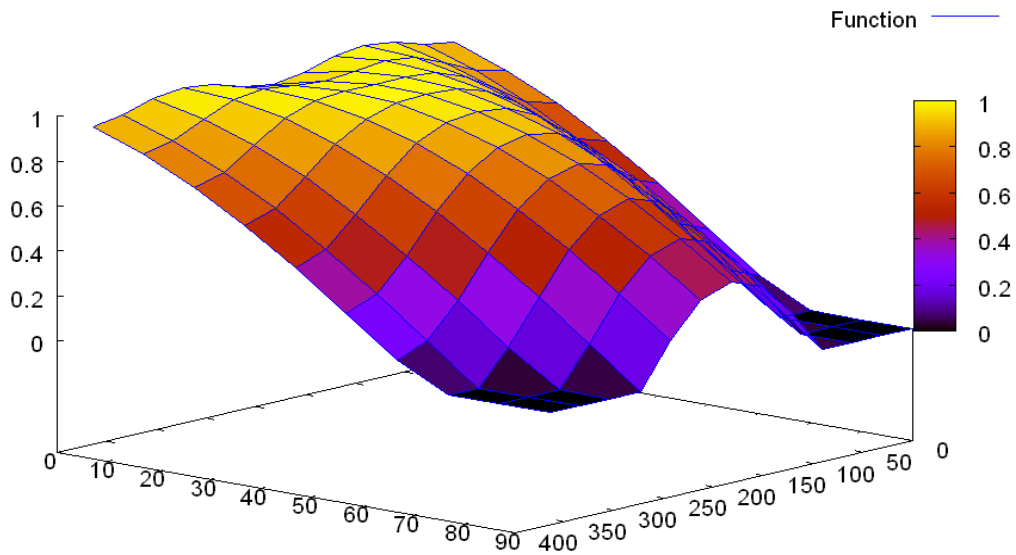
Appendix 1: $\mathcal{R}(t, x; s = \phi = 0, 3, 6, 9, \dots, 21)$: Xmaxima graph plotting program format.

```

*****
plot3d(0.5*abs(sin(%pi/2+asin(sin(0.408)*cos(2*%pi*t/365)))*sin(%pi/2-%pi*x/180)
*cos(2*%pi*s/24)+cos(%pi/2+asin(sin(0.408)*cos(2*%pi*t/365)))
*cos(%pi/2-
%pi*x/180))+0.5*(sin(%pi/2+asin(sin(0.408)*cos(2*%pi*t/365)))*sin(%pi/2-
%pi*x/180)
*cos(2*%pi*s/24)+cos(%pi/2+asin(sin(0.408)*cos(2*%pi*t/365)))
*cos(%pi/2-%pi*x/180)), [t, 0, 365], [x, 0, 90], [grid, 12, 9]);
*****

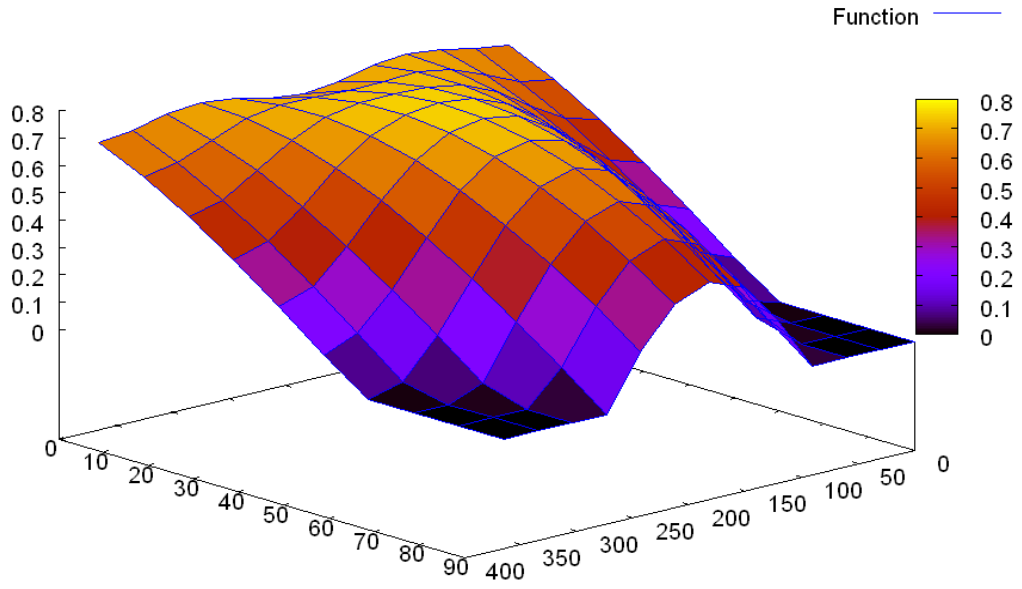
```

$\phi = 0/24$.



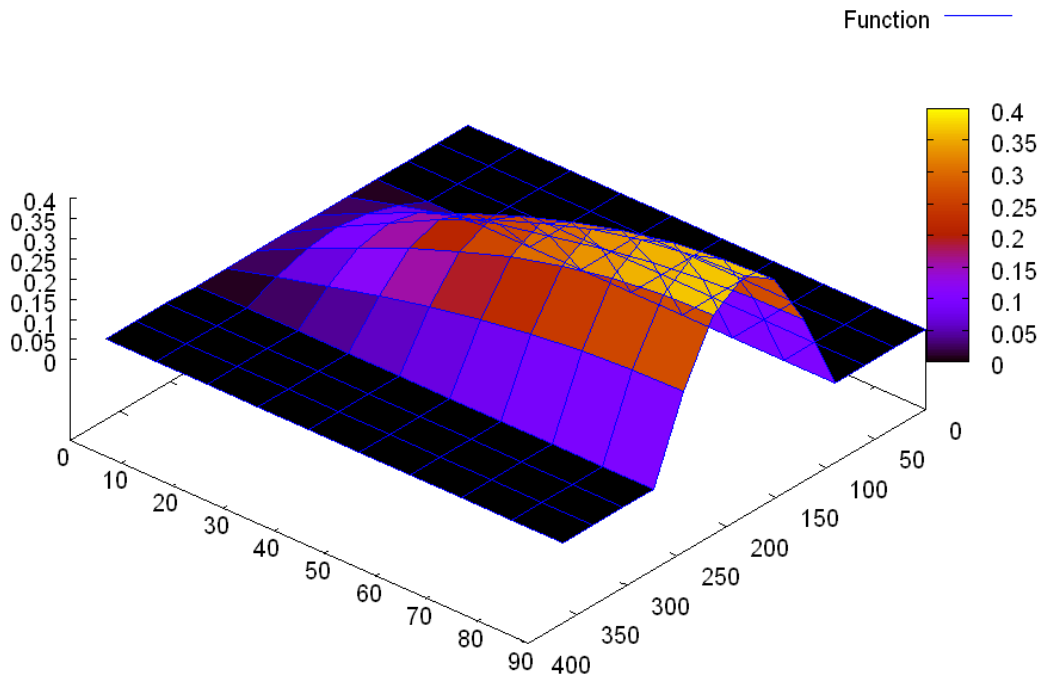
view: 70.0000, 131.0000 scale: 1.00000, 1.00000

$\phi = 3/24$.



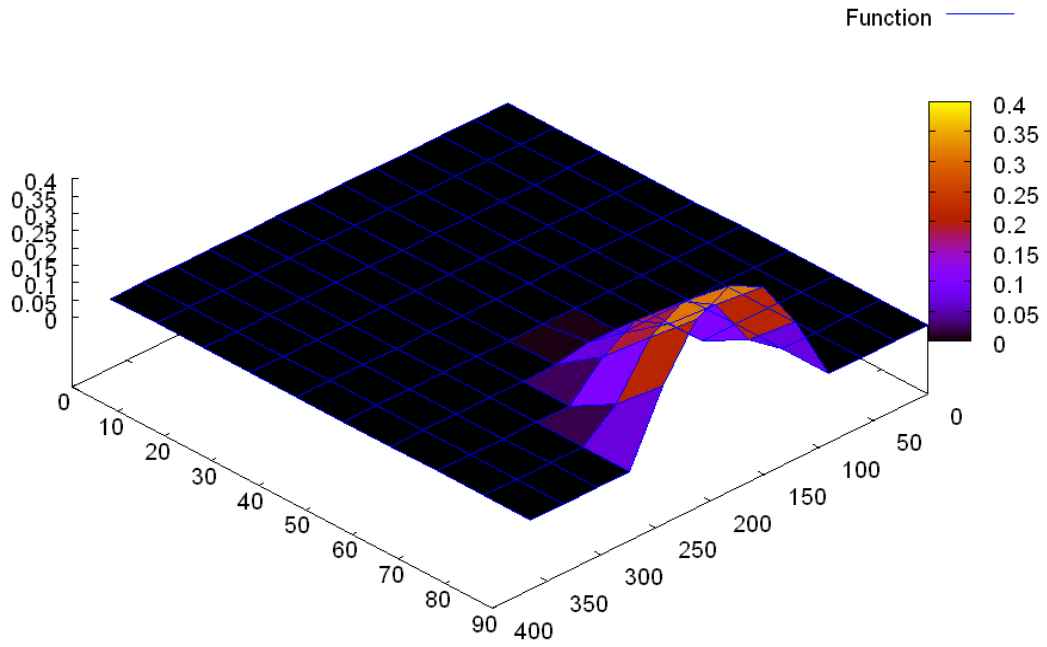
view: 64.0000, 138.000 scale: 1.00000, 1.00000

$\phi = 6/24$.



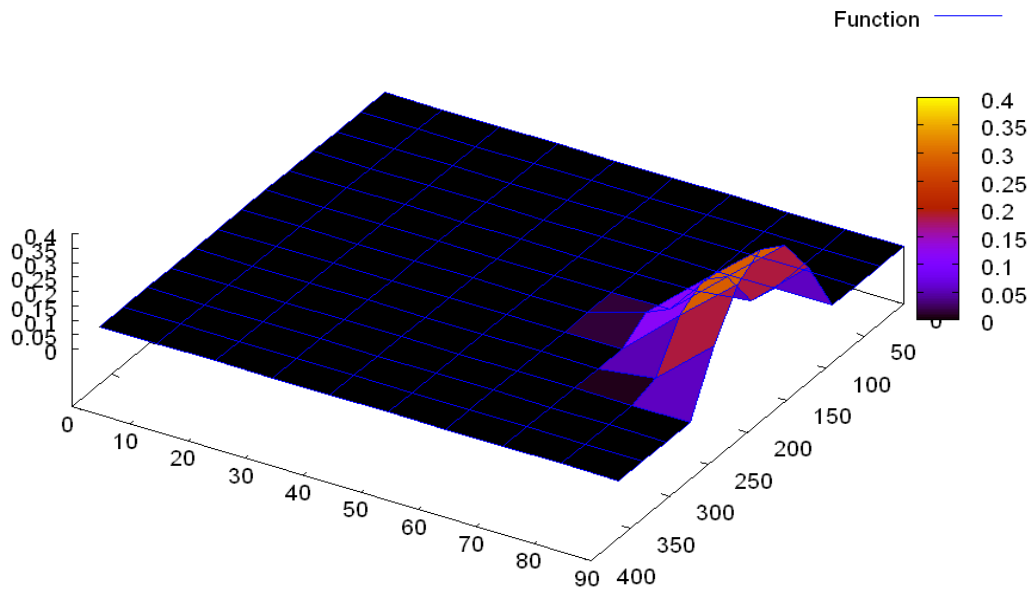
view: 38.0000, 131.000 scale: 1.00000, 1.00000

$$\phi = 9/24.$$



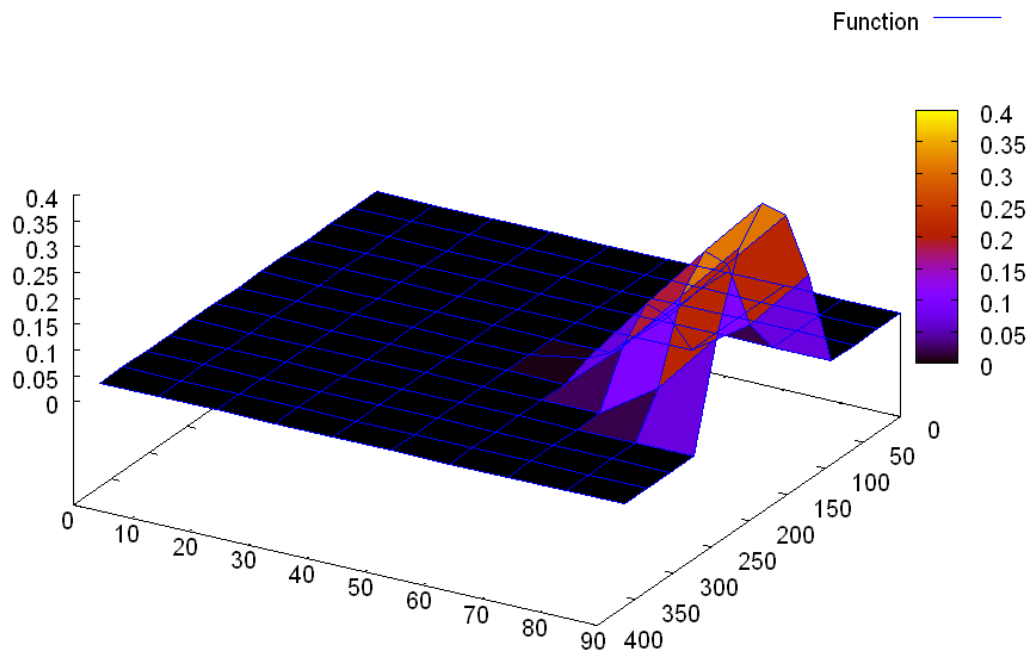
view: 34.0000, 136.000 scale: 1.00000, 1.00000

$$\phi = 12/24.$$



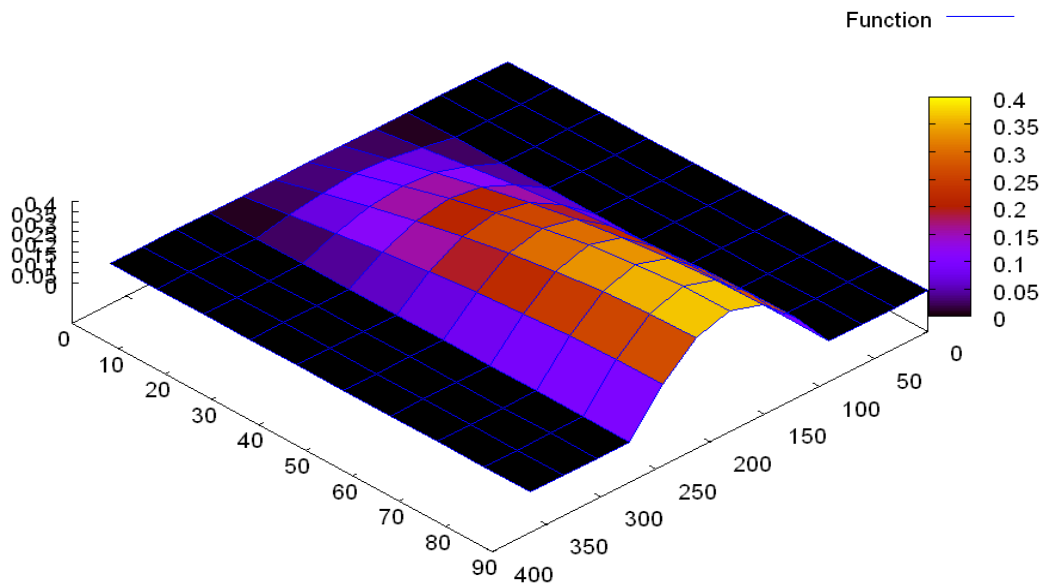
view: 30.0000, 121.000 scale: 1.00000, 1.00000

$$\phi = 15/24.$$



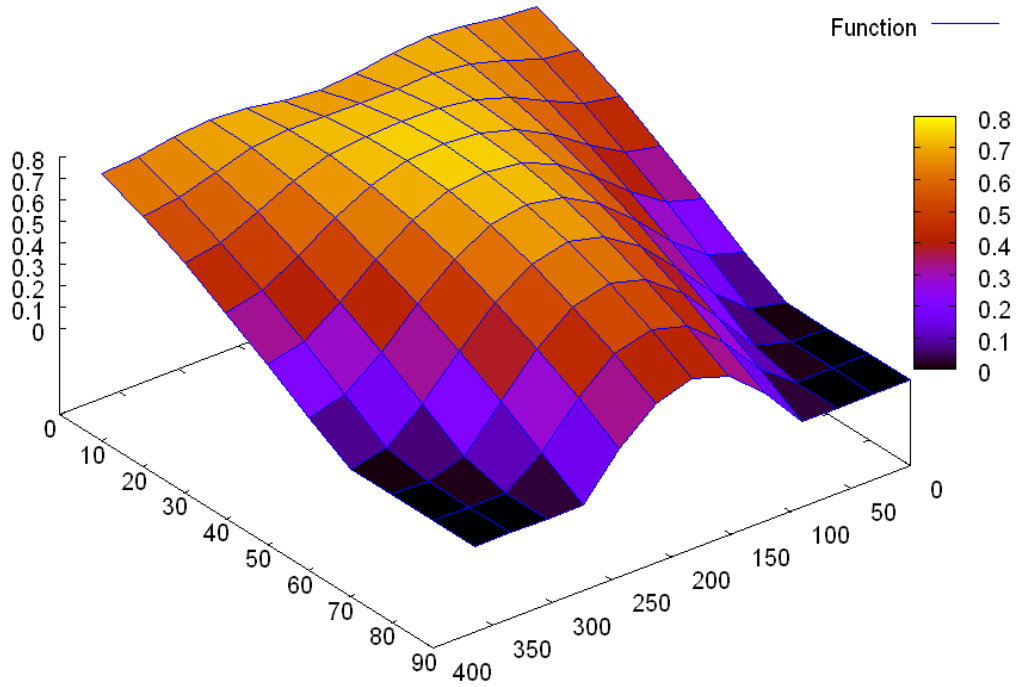
view: 52.0000, 120.000 scale: 1.00000, 1.00000

$$\phi = 18/24.$$



view: 21.0000, 136.000 scale: 1.00000, 1.00000

$$\phi = 21/24.$$



view: 41.0000, 142.000 scale: 1.00000, 1.00000

The rogo mark of REAL CLIMATE : <http://www.realclimate.Org/>

