

## Unless Drastic Counter Measure, Arctic Ice Lid Vanish would Become Catastrophic.

Unless drastic and emergent global counter measure, it is certain we would be extincted in few decades !!!.

2011/11/27, 12/4,7

### NOTIFICATION:

Following are correction on Arctic Ocean Heat Capacity in following site.

Author made terrible mistaking **1/10 smaller Heat Capacity of Arctic Ocean**,

however now, which became no substantial trouble in the scientific essence,

however it could become **supreme trouble** for mankind and other species.

Author entirely wish global wisdoms of you all !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!

[http://www.777true.net/GLOBAL-DECLARATION-WAR-on-CARBON-with-Geo\\_Engineering\\_Part\\_C.ppt](http://www.777true.net/GLOBAL-DECLARATION-WAR-on-CARBON-with-Geo_Engineering_Part_C.ppt)

\*incomplete photos p12, 15, 16 are supplemented in this last pages.

(1) Arctic ocean area (above latitude  $70^\circ$  ).

\*area =  $1.409 \times 10^{13} \text{m}^2$  (author's error is  $1.409 \times 10^{12} \text{m}^2$  !!!) .

<http://www.oceansatlas.com/unatlas/about/physicalandchemicalproperties/background/seemore1.html>

\*area =  $9.5 \times 10^{12} \text{m}^2$  (right). Area above  $70$  latitude must be subtracted by area of Greenland and other islands.

<http://ja.wikipedia.org/wiki/%E6%B5%B7>

(2) water specific heat =  $4.178 \text{KJ/Kg.K}$  is not right, salty degree is 10 times larger in Arctic, then we could derive salty sea water  $2.85 \text{KJ/Kg}$ .

[http://detail.chiebukuro.yahoo.co.jp/qa/question\\_detail/q1265159167](http://detail.chiebukuro.yahoo.co.jp/qa/question_detail/q1265159167)

(3) Arctic ocean depth and methane clathrate reservoir distribution ( $200 \sim 1200 \text{m}$ ).

<http://www.marinebio.net/marinescience/04benthon/arcocean.htm>

You could see that almost half of Arctic ocean floor is shallow as  $300 \sim 600 \text{m}$  depth, in which almost MC reservoir seems to lie. Then depth  $1255 \text{m}$  is too deep.

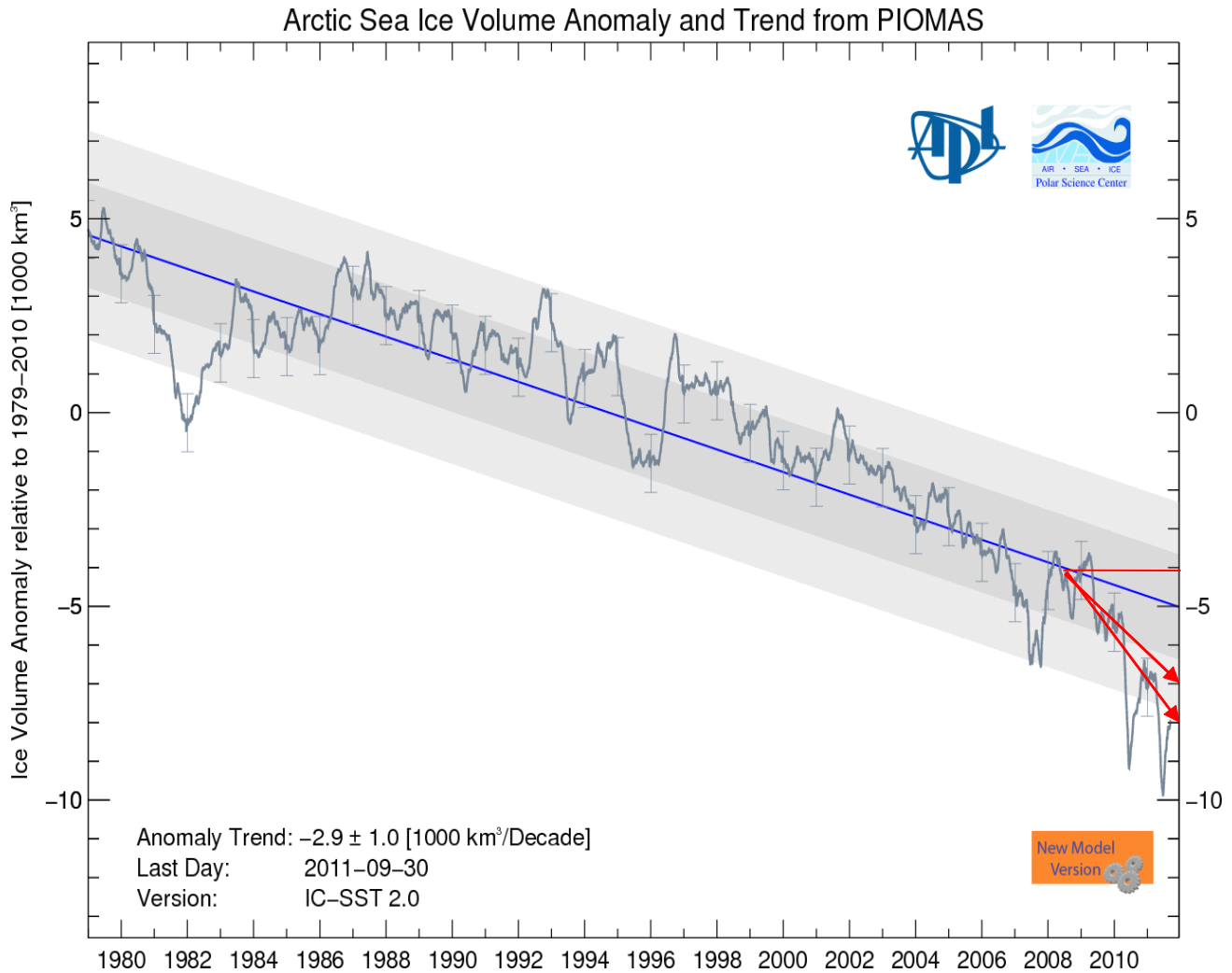
(4) **Arctic Ocean Heat Capacity  $C_A = 3.3 \times 10^{22} \text{J/K}$**  (depth  $1200 \text{m}$ ).

$$C_A = 9.5 \times 10^{12} \text{m}^2 \times 1200 \text{m} \times 1020 \text{kg/m}^3 \times 2.85 \text{KJ/Kg} = \mathbf{3.3 \times 10^{22} \text{J/K}}$$

**Part I :The fate of Arctic Ice lid.**

[ 1 ] : How much heat input for melting ice lid.

[1]:Data Reveals Ice Albedo Feedback Causing **Abrupt Heat Input Rise in Arctic.**



Ice decreasing amount/year is equivalent to melting heat input = P<sub>m</sub> in to the ice.

(1)ice melting heat = 334.7 kJ/kg

(2)ice density = 0.917 g/cm<sup>3</sup> = 0.917 kg/m<sup>3</sup>

(3)ice decrease/y = 2.9 x 10<sup>11</sup> km<sup>3</sup>/y = 2.9 x 10<sup>11</sup> x 1000<sup>3</sup> m<sup>3</sup>/y = 2.9 x 10<sup>14</sup> m<sup>3</sup>/y = 2.66 x 10<sup>11</sup> kg/y.

(4)melt heat/y (1978~2006)  $\hat{=}$  2.66 x 10<sup>11</sup> kg/y x 334.7 kJ/kg = 8.9 x 10<sup>19</sup> J/y  $\equiv$  P<sub>o</sub>.

This may be mainly due to Pacific and Atlantic ocean heat input.

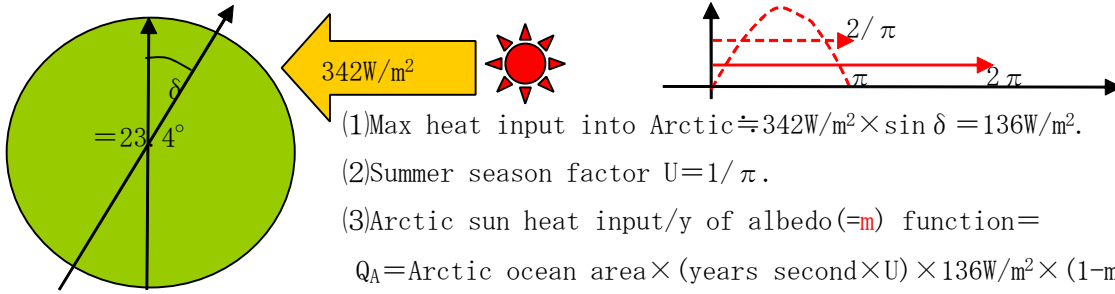
(5)melt heat/y (2006~2011)  $\hat{=}$  4.5 x 8.9 x 10<sup>19</sup> J/y = 4 x 10<sup>20</sup> J/y  $\equiv$  P<sub>m</sub>.

Note ice temperature rise heat is no concerned. So the actual heat input is larger than P<sub>m</sub>.

(6) Sudden decline at 2006~2008 may be beginning of **ice albedo feedback**.  
 Summer **opened black sea mouth** absorb more sun heat, which is to accelerate more ice vanishing. This become ominous positive feedback. See P4 in the below.

**[2]: How much Heat Input Rise ? at Albedo Feedback. Saturation of Ice Lid Vanishing Time.**

Following are rather wild estimation, so you should read carefully.



- (1) Max heat input into Arctic  $\doteq 342\text{W/m}^2 \times \sin \delta = 136\text{W/m}^2$ .
- (2) Summer season factor  $U = 1/\pi$ .
- (3) Arctic sun heat input/y of albedo (=m) function =  
 $Q_A = \text{Arctic ocean area} \times (\text{years second} \times U) \times 136\text{W/m}^2 \times (1-m)$   
 $= 9.5 \times 10^{12} \text{m}^2 \times (3600 \times 24 \times 365) U \times 136\text{W/m}^2 (1-m) = (1-m) 1.3 \times 10^{22} \text{J/y}$ .

(4)  $\Delta Q_A = 1.3 \times 10^{22} \text{J/y} (-\Delta m) = \text{heat input rise by albedo down} = \Delta m$ .

(5) Estimation on albedo down =  $\Delta m$  at current (2011) trend of  $P_m$ .

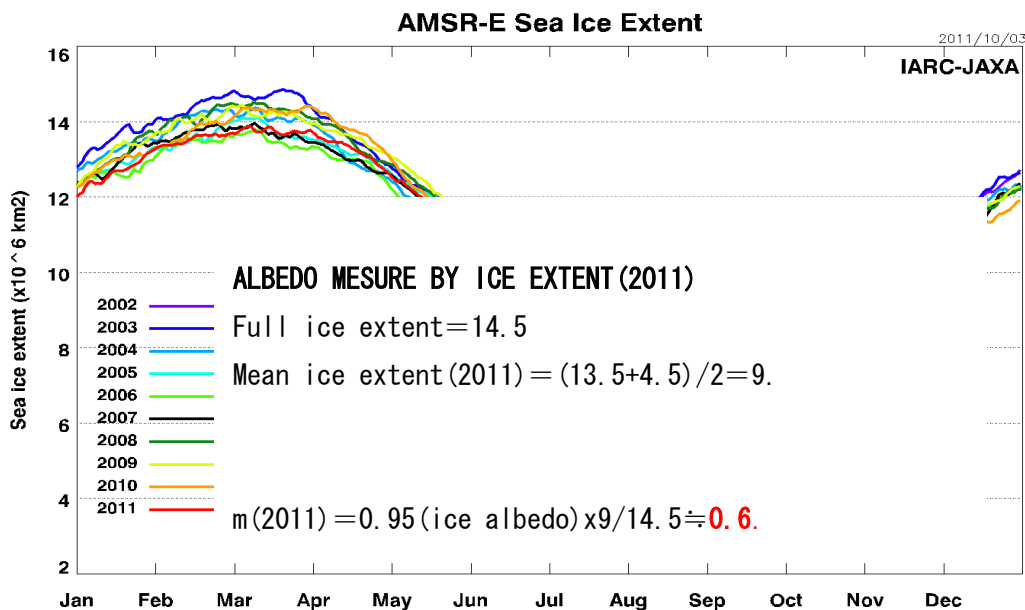
$\Delta Q_A = 1.3 \times 10^{22} \text{J/y} (-\Delta m) = P_m - P_o (\text{ocean heat input}) \doteq 4 \times 10^{20} \text{J/y} - 1 \times 10^{20} \text{J/y}$   
 $\rightarrow \Delta m \doteq 0.023$ .

(6) **albedo change with the input- heat- rise.** saturation point

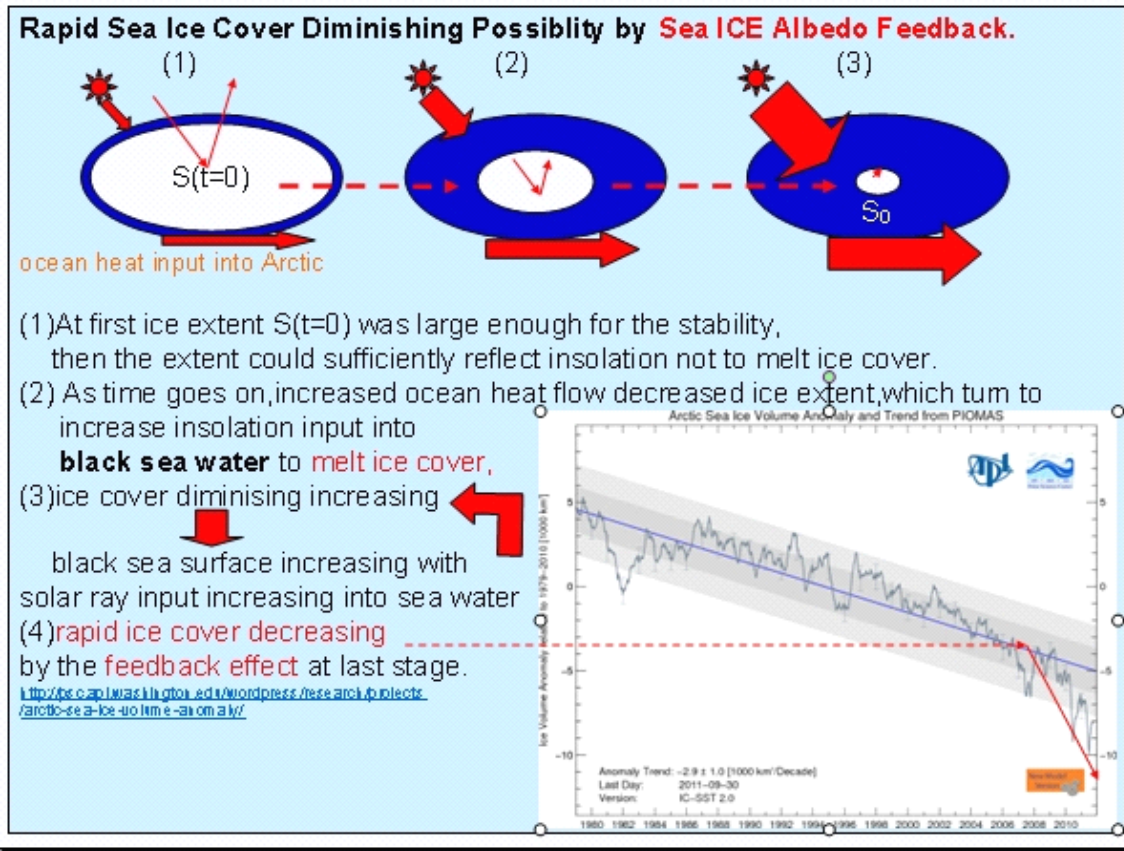
$\Delta m \doteq -0.023$		$\Delta m \doteq -0.23$	$\Delta m \doteq -0.6$
$\Delta Q_A = 3 \times 10^{20} \text{J/y}$	→	$3 \times 10^{21} \text{J/y}$	$7.8 \times 10^{21} \text{J/y} ?!$

(7) Ice Extent Data: Max =  $1.4 \times 10^{13} \text{m}^2$ . Min =  $0.5 \times 10^{13} \text{m}^2 \doteq 30\%$  at 2011.

[http://www.ijis.iarc.uaf.edu/en/home/seaice\\_extent.htm](http://www.ijis.iarc.uaf.edu/en/home/seaice_extent.htm)



[ 3 ]:Arctic Ice albedo feedback causing rapid ice vanishing and heat input rise.



(1):The Cause of Rapid Melt by Albedo Feedback.

Ice lid melt amount(area)/year( $dS(t)/dt$ ) is proportional to heat input into ice/year, which is also proportional to solar input to opened mouse sea area =  $(S(t) - S_0)$ . Hence we derive,

$$* (dS(t)/dt) = k(S(t) - S_0) \equiv (S(t) - S_0) / \tau .$$

$$\rightarrow dS/dt - kS = -kS_0. \rightarrow d(S \exp(-kt)) / dt = -kS_0 \exp(-kt).$$

$$S(t) = -S_0 \exp(kt) \int_0^t du \langle \exp(-ku) / du \rangle + C \exp(kt).$$

$$= -S_0 \exp(kt) [\exp(-ku)]_0^t + C \exp(kt) = S_0 + (C - S_0) \exp(kt).$$

$$\rightarrow S(t=0) = S_0 + (C - S_0). \rightarrow C \equiv S_0 - \delta. \rightarrow \delta \text{ is something small constant.}$$

$$* S(t) = S_0 - \delta \exp(kt) \equiv S_0 - S(tm) \exp(\langle t - tm \rangle / \tau). \langle S(tm) \equiv \delta \exp(ktm) \rangle$$

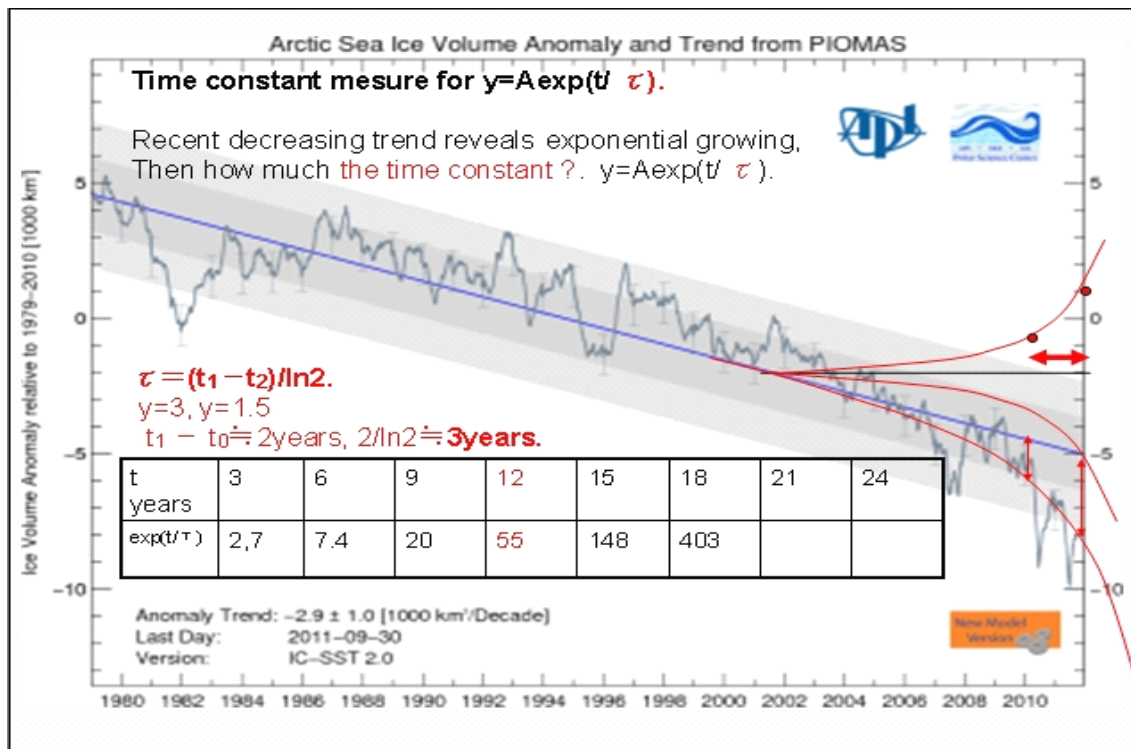
verification:  $dS/dt = -\delta' \exp(kt) - k \delta \exp(kt) = -k \delta \exp(kt) = k(S(t) - S_0)$ .

(2):  $\{S(tm), \tau\}$  are observable value by recent data.

$$y = A \exp(t / \tau). \rightarrow \{y_1 = A \exp(t_1 / \tau), y_2 = A \exp(t_2 / \tau) \equiv 2y_1\}$$

$$\tau = (t(y_2) - t(y_1)) / \ln 2.$$

(3) Time constant  $\tau$  measure and the ice lid fate with exponential growing heat.



(4) time for ice lid zero  $\equiv t_z$  with the max albedo radiative forcing in Arctic.

The ice melt amount years function  $Y(t)$  may be  $Y(t) = A\exp(t/\tau) + Bt + C$ . Then  $dY(t)/dt = \text{ice volume decrease/year} = \text{melting heat input}/y(\text{albedo feedback})$ .

\*  $P(t) = (A/\tau)\exp(t/\tau) + B \doteq (A/\tau)\exp(t/\tau)$ .  $\langle B(\text{ocean heat}) \text{ is smaller} \rangle$

That is, heat input is also exponential growing with the same time constant  $\tau$ .

$P_m(2007 \sim 2011) \doteq 3 \times 10^{20} \text{J/y}$ . (minus ocean heat  $= 1 \times 10^{20} \text{J/y}$ )

$P_m(\Delta m \doteq -0.6) \doteq 7.8 \times 10^{21} \text{J/y} \equiv P_z$ . (max albedo radiative forcing at  $m=0$ : zero ice lid)

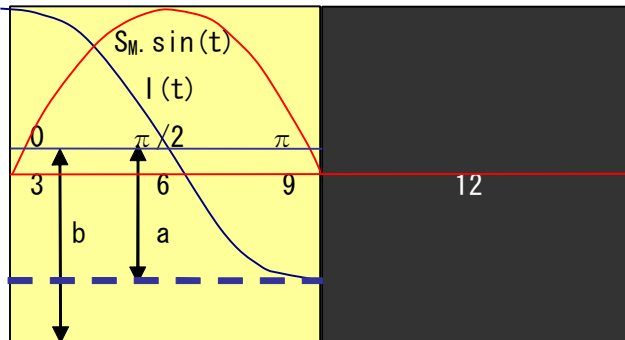
Time for  $(7.8 \times 10^{21} \text{J/y} / 3 \times 10^{20} \text{J/y}) \doteq 26$  times (time for ice lid zero  $\equiv t_z$ ) is about  $t_z = 10 \text{ years} \pm$  "climate fluctuation width" ? in exponential growth.

(5) Time for whole Arctic ocean  $1^\circ\text{C up} = C_A/P_m$ .  $\langle C_A = 3.3 \times 10^{22} \text{J/K}$ . see p1  $\rangle$

$P_m(\Delta m \doteq -0.023)_{2011}$	$P_m(\Delta m \doteq -0.23)_{2018}$	$P_m(\Delta m \doteq -0.40)_{2019}$	$P_m(\Delta m \doteq -0.6)_{2021}$
radiative forcing			26W/m <sup>2</sup> .
$3 \times 10^{20} \text{J/y}$ .	$3 \times 10^{21} \text{J/y}$	$5.2 \times 10^{21} \text{J/y}$	$7.8 \times 10^{21} \text{J/y}$
110y	11y	6.3y	4.2y

This is valid only when exponential growth of constant  $\tau$  is right.

**Appendix1: Arctic annual heat input =  $Q_A$  by sea ice albedo =  $m$ .**



\*  $S_M \sin(t)$   $\equiv$  seasonal solar heat.  
 \*  $I(t) \equiv a \cos(t) + b$ .  
 $\equiv$  ice extent.  $A_0 \equiv$  ocean area.  
 \*  $S_M \equiv$  max solar input into Arctic  
 $= 342 \text{ W/m}^2 \cdot \sin(23.4^\circ \text{C}) = 136 \text{ W/m}^2$ .  
 \*  $b \equiv$  center value of ice  
 extent/max,  $\lambda \equiv$  ice albedo  $\sim 0.95$ .

(a)  $Q_A \equiv$  year averaged heat input in Arctic  $\equiv$  mean solar heat  $(1 - \text{albedo}) = (S_M / \pi) (1 - m)$   
 $= (1 / 2\pi) \int_0^\pi dt S_M \sin(t) [A_0 - \lambda (a \cos(t) + b)] / A_0$   
 $= (S_M (1 - b') / 2\pi) \int_0^\pi dt \sin(t) = S_M (1 - b') / \pi \equiv (S_M / \pi) (1 - m)$ .  
 $1 - m = 1 - b' \rightarrow m = 0.95$  (ice surface albedo =  $\lambda$ )  $b$ .

(b) remain albedo (2011)  $\doteq 0.95 \times (13.5 + 4.5) / 2 \times 13.5 = 60\%$ .

## Part II : A coarse estimation on the Arctic Methane Catastrophe.

Once ice lid had vanished, and sea water temperature would rise, irreversible and catastrophic methane catastrophe would begin in decades year range.

Following are a simple model analysis, but it may grasp the perspective mechanism. You should carefully examine **the causality chain**. 2011/11/30, 12/5

### [ 0 ] : Physical Basis with the "perspective and averaged" view point.

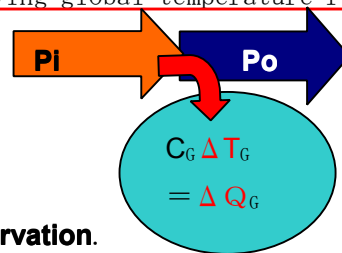
(1) Radiative Forcing (DEBT HEAT in year budget) driving global temperature rise.

(a) **debt heat (~radiative forcing)/year**

$$= \text{incoming heat/y} - \text{outgoing heat/y} (\Delta Q \equiv dQ/dt).$$

(b) **heat capacity ( $\equiv C$ )  $\times$  temperature rise ( $\Delta T \equiv dT/dt$ )**

$$= \text{input heat increase} (\Delta Q) ; C \Delta T = \Delta Q.$$



This is the 1st law of thermodynamics **energy conservation**.

☞ : Global ocean's annual dynamic heat capacity ( $C_G$ ) depth is almost 600m.

$$C_G (dT_G/dt) = U \pi R_G^2 F_0 (1-m) - U 4 \pi R_G^2 \sigma T_G^4 = (U \times 4 \pi R_G^2) F.$$

**Global Debt Heat Rise/y = Insolation input/y - Radiation output/y = Radiative Force.**

\* @  $\equiv$  Space passing probability of cooling radiation ( $\sigma T_G^4$ ) due to GHG density.

\*  $(U \times 4 \pi R_G^2) = 3600 \times 24 \times 365 \text{sec} \times \text{global area (m}^2\text{)}.$

\*  $F_0(1-m) = \text{solar input} \times (1 - \text{ray reflection rate (albedo)}).$

(c) global and years averaged view point:

**(ensemble averaging reducing random noise).**

In local view point, there are **random variations** at anywhere anytime, however, global and years perspective view is to reveal simple and accurate causal tendency.

(d) Professional Global Circulation Model has a defect.

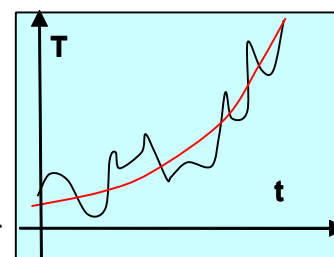
You could see **smoke flow trajectory** clearly at first, however as time goes on, those would disappear due to microscopic molecular random collisions (**diffusion**).

$$m d\mathbf{V}/dt = \mathbf{f} \rightarrow \rho (D\mathbf{V}/Dt) = \mathbf{f} - k \nabla^2 \mathbf{V} - \text{grad } P + \rho \mathbf{g} \ll \text{Fluid Dynamic Equation} \equiv \text{FDE} \gg$$

☞ :  $k \nabla^2 \mathbf{V}$  is **inter-fluid friction force** term causing trajectory disappearing in long time.

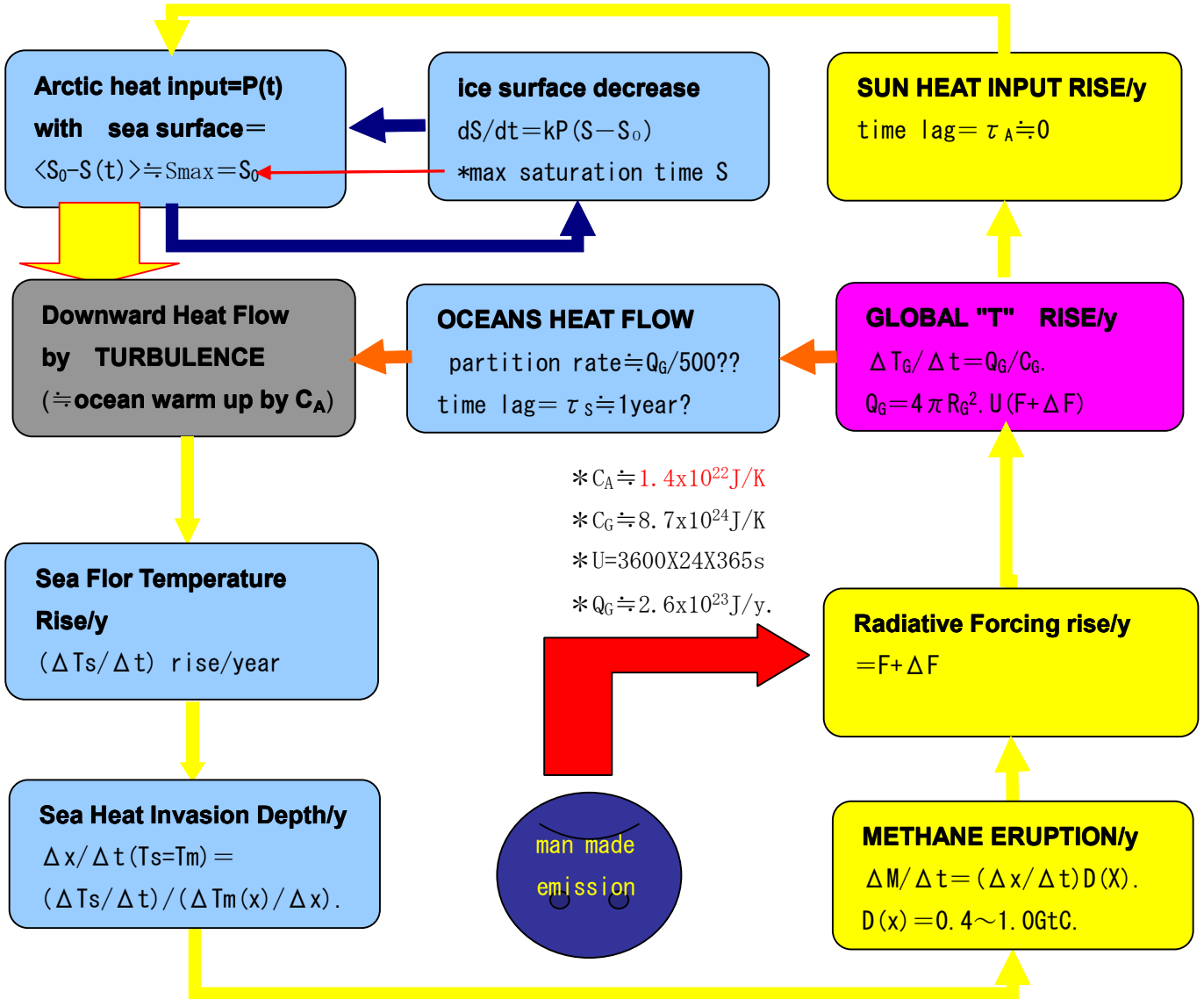
Weather forecasting is accurate in short days, but becomes uncertain as day longer.

This is essentially due to **the nature-itself (chaos)**, but not due to defect of science. A climate dynamics has an uncertainty due to those reason. Therefore, in



possible some cases, we had better to take another method without FDE.

[ 1 ] : OCEAN, ICE ALBEDO, METHANE- FEEDBACK PROCESS AROUND ARCTIC.





**[ 2 ] : Instant Sea Flor Heat Transfer Model in the long time range:**

(1) **Melting Heat Invasion Depth**  $\equiv x(t)/\text{year}$ :

$$dx(t)/dt = (dT_s(x, t)/dt) / (dT_m(x)/dx). \langle\langle T_s = T_m \rangle\rangle$$

(2) **Methane Melting Amount/year in the one dimensional distribution** =  $D(x)$ .

$$dM(t)/dt = D(x) (dT_s/dt) / (dT_m/dx). \langle\langle dM(t)/dt = D(x) \langle dx/dt \rangle \rangle\rangle$$

\*  $D(x) \equiv$  Methane Clathrate Distribution Density at depth  $x=0.4 \sim 1.0 \text{GtC/m}$ .

(3) **Sea Temperature Rise/year by Radiative Forcing by Ice Albedo(m) and Methane(@).**

$$C_A (dT_s(t)/dt) = US (F_m(t) + \Theta F_\oplus(t)).$$

Note right term is heat input on sea surface at time=t, and left is temperature rise of sea floor to where heat transfer takes finite time delay  $\tau(x, t)$  in actual, however, we take  $\tau(x, t) \doteq 0$  approximation in global scale time constant (10 years).

\*  $F_\oplus \equiv$  Radiative Forcing by CH4 and that by CO2.  $\langle\langle$  This is global  $\rangle\rangle$

As for Arctic, RF local factor  $\equiv \Theta = (\langle T_A^4 \rangle / \langle T_G^4 \rangle)$  must be multiplied.

\*  $F_m \equiv$  Radiative Forcing by Arctic Ice Albedo ( $\equiv m$ ) Change =  $-F_0 \Delta m$ .  $\langle$  This is local  $\rangle$

\*  $S \equiv$  Area of Arctic Ocean with Methane Clathrate Reservoir in the sea floor.

\*  $U \equiv 3600 \times 24 \times 365 \text{s} = \text{years time by second}$ .

\*  $T_s(x, t) \equiv$  sea floor temperature of melting point  $x \doteq T_s(t)$ .

$\Rightarrow$  : Actual  $T_s$  is depth=x and time=t dependent complicated function with time delay of heat input at sea surface, however, we take a **wild approximation** of depth uniform model without the time delay in long time constant view (10 years).

\*  $C_A \equiv$  Dynamic Heat Capacity of Arctic Ocean with Methane Clathrate Reservoir.

$\Rightarrow$  : Global ocean's annual dynamic heat capacity ( $C_G$ ) depth is almost 600m.

$$C_G (dT_G/dt) = U \pi R_G^2 F_0 (1-m) - U 4 \pi R_G^2 \Theta \sigma T_G^4 = (U \times 4 \pi R_G^2) F.$$

**Global Debt Heat Rise/y = Insolation input/y – Radiation output/y = Radiative Force.**

\*  $\Theta \equiv$  Space passing probability of cooling radiation ( $\sigma T_G^4$ ) due to GHG density.

(4) **Methane Radiative Forcing  $\equiv F_\oplus(t)$  > Evolution Equation.**  $\langle\langle \Gamma(M) \equiv dF_\oplus/dM \rangle\rangle$

$$dF_\oplus/dt \equiv \Gamma(M) dM/dt = [\Gamma(M) D(x) / (dT_m/dx)] (dT_s/dt) = [\Gamma D / (dT_m/dx)] \langle US/C_s \rangle (F_m + \Theta F_\oplus) \\ = [\Gamma D / (dT_m/dx)] \langle S/C_s \rangle F_m + [\Gamma D / (dT_m/dx)] \langle S/C_s \rangle F_\oplus.$$

$$(5) dF_\oplus/dt - [\Gamma D(x) / (dT_m/dx)] \langle US/C_s \rangle \Theta F_\oplus = [\Gamma D(x) / (dT_m/dx)] \langle US/C_s \rangle F_m.$$

$$(6) dF_\oplus/dt + f F_\oplus = g.$$

$$(7) F_\oplus(t) = \int_0^t du g(u) \exp(-\int_u^t dv f(v)) + C \exp(-\int_0^t du f(u)).$$

$$(8) f \equiv [\Gamma D(x) / (dT_m/dx)] \langle US/C_s \rangle \equiv \Theta / \tau.$$

$$(9) g \equiv [\Gamma D(x) / (dT_m/dx)] \langle US/C_s \rangle F_m \equiv F_m / \tau.$$

**[ 3 ] : Wild Estimation on the Time Constant of Exponential Growth.**

$[\Gamma(M) D(x) / (dT_m(x) / dx)] < US / C_s > \equiv 1 / \tau .$

U ≡ years time by second.	3600x24x365s = 31536000s.
S ≡ Arctic ocean area for RF input <a href="http://ja.wikipedia.org/wiki/%E6%B5%B7">http://ja.wikipedia.org/wiki/%E6%B5%B7</a>	0.95X10 <sup>13</sup> m <sup>2</sup> . US = 3x10 <sup>20</sup> m <sup>2</sup> s. ★
C <sub>s</sub> ≡ Arctic ocean dynamic heat capacity S = 0.95X10 <sup>13</sup> m <sup>2</sup> . ρ p = density × specific heat = 1020kg/m <sup>3</sup> × 2.85KJ/Kg	C <sub>s</sub> (300m) = 0.83x10 <sup>22</sup> J/K C <sub>s</sub> (400m) = 1.1x10 <sup>22</sup> J/K C <sub>s</sub> (500m) = 1.4x10 <sup>22</sup> J/K C <sub>s</sub> (1200m) = 3.3x10 <sup>22</sup> J/K
D(x) ≡ MC distribution density	0.4 ~ 1.0GtC/m (x = 200 ? ~ 1200m)
1 / (dT <sub>m</sub> /dx) ≡ melt heat gradient ★	≐ 1600m/70°C (x = 300m) → 23 ≐ 1600m/45°C (x = 400m) → 36 ≐ 1600m/30°C (x = 500m) → 53
★ dF(M) / dM ≐ 0.39 / √M. <a href="#">F = 0.036(√(472M) - √700ppb) - δ.</a> Γ(M) ≡ dF/dM ≡ RF gradient by M. 1900ppb (2011) / 472 = 4GtC (2011) <<1GtC = 472ppb>> dM/dt ≐ 0.02GtC/y (2011).	M = 4 → 0.2 → x 0.3 ~ 0.8 → 6 ~ 17y M = 14 → 0.10 → x 0.3 ~ 0.8 → 13 ~ 33y M = 24 → 0.08 → x 0.3 ~ 0.8 → 16 ~ 42y M = 34 → 0.07 → x 0.3 ~ 0.8 → 18 ~ 48y  M = 100 → 0.04 → x 0.3 ~ 0.8 → 31 ~ 83y  M = 200 → 0.03 → x 0.45 ~ 1.13 → 30 ~ 74y
τ ≡ Radiative Forcing Rise Time. [ Γ(M(t)) D(x(t)) / (dT <sub>m</sub> /dx) ] < US / C <sub>s</sub> > ≡ 1 / τ .	<b>5y &lt; τ &lt; 50y</b>

★ ≡ almost reliable.

\*F<sub>m</sub> ≐ 26W/m<sup>2</sup>; initial dominant factor due to max ice albedo radiative forcing [3](5).

dF<sub>@</sub>/dt = (F<sub>m</sub> + ΘF<sub>@</sub>) / τ. <this is only valid in Arctic, but not in global>

\*Note radiative forcing **F<sub>@</sub> = 1.6W/m<sup>2</sup>** is equivalent to heat up earth ΔT/Δt ≐

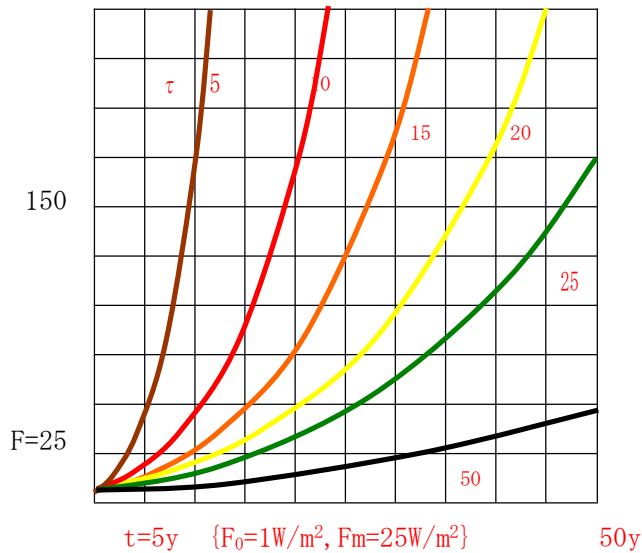
**0.03°C/y** and also global ocean temperature rise is the same.

\*time(ice lid vanish) → ice albedo max radiative forcing F<sub>m</sub>(Arctic) = 26W/m<sup>2</sup>.

dF<sub>@</sub>/dt = (F<sub>m</sub> + ΘF<sub>@</sub>) / τ ≐ 26W/m<sup>2</sup> / (5y ~ 50y).



<http://www.realclimate.org/>



$$F_{@} = \int_0^t du g(u) \exp\left(-\int_u^t dv f(v)\right) + C \exp\left(-\int_0^t du f(u)\right)$$

$$= F_m \cdot \exp(t/\tau) [1 - \exp(-t/\tau)] + F_0 \exp(t/\tau).$$

Note that there could be no possibility to eliminate essential dangerous fact even by time and intensity scaling change with multiplying 2, 1/2 or 3, 1/3.  
 This is the essential danger of exponential growing by positive feedback.

**Disucussion:**

People must be awoken by this ominous climate fact right now.

**The last betting may be geo-engineering with 80% CO2 cutting right now !**

Author entirely wish global wisdoms of you all !!!!!!!!!!!!!!!!!!!!!!!!!!!!!!!.