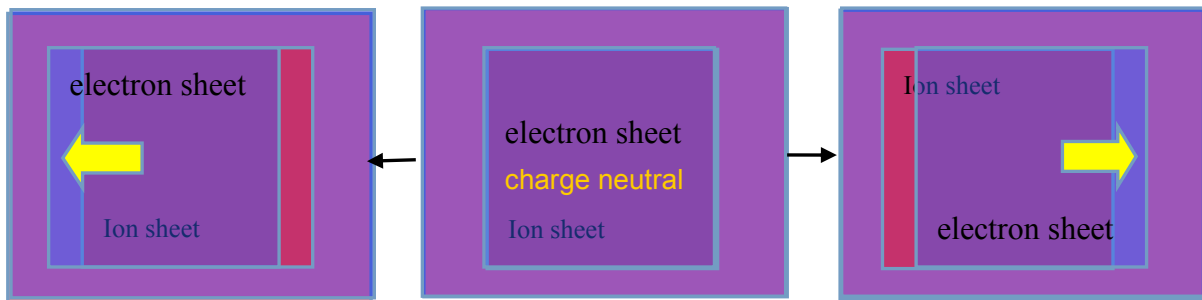


Charge Alternating by Plasma Oscillation Resonance. 2016/6/15,16,20,21,22,24.

Electron Charge Density $N_e(x,y,z)$ is increasing function of height $=z$ till ion sphere summit. Usually, $N_e(x)$ are overlapped with ion density $N_i(x)$ as charge neutral law ($0 = N_i(x) - N_e(x)$). By making light mass electrons shifts by $x \pm \delta x$, then $\pm \delta x N_e(x) < 0, > 0$. Such charge emerging (with kinetic inertia) act to recover charge neutral state. This become **plasma oscillation** $= \omega_p$. If irradiating such **density layer** by same frequency $\omega = \omega_p$, from ground beam radiator, **the resonance** can generate **alternate charge density wave (CDW)** toward ground. However, this horizontal modulation (x,y) could not be large CDW antenna. While, vertical modulation (z) could be large CDW antenna (HAARP?!!!).

[1] : *Plasma Lecture Notes.*

<http://www.pp.teen.setsunan.ac.jp/lecture/#lec12>



electron left shift <this is a **accordion** model, but not harp>

electron right shift

Left figs are **very simplified Plasma Self Oscillation MODEL**..x is horizontal position (also **displacement**) variable of electrons. Heavy weight **ion (red sheet)** is not movable by electric intensity $= E$. While light weight electrons is to shift left and right by E . Note $\oint \mathbf{dS} = Q$ is *Gauss's law* for volume charge $= Q$. n_0 is electron volume density. S is perpendicular surface area of sheet.

Plasma Self Oscillation. $\langle m_e = \text{electron mass} \rangle$

$$E = Q / \epsilon S = e n_0 x S / \epsilon S = e n_0 x / \epsilon.$$

$$m_e (d^2 x / dt^2) = E e = - e^2 n_0 x / \epsilon.$$

$$X(t) = A \cos(\omega_p t). \quad \omega_p = \sqrt{(e^2 n_0 / m_e \epsilon)}.$$

$$m_e (d^2 x / dt^2) = - e E_0 \cos(\omega t) - e^2 n_0 x / \epsilon.$$

$\Rightarrow \omega = \omega_p$ is **strong resonance** between plasma and EM wave. Then note charge term $e^2 n_0 x / \epsilon$ is also **strong resonance**. This could be alternate charge density wave source $= \rho$ toward ground !!! \rightarrow

$$\square \phi = - \rho / \epsilon.$$

EM wave excitation.

$$A = (e E_0 / m_e) / (\omega^2 - \omega_p^2).$$

$$E = E_0 \cos(\omega t) \omega^2 / (\omega^2 - \omega_p^2).$$

[2] : Full Set(?) Dynamic Equation of Electron in Ion Sphere.

2016/6/15,16,17

Here is the kernel of **CDW generating mechanism** in **electron resonance dynamics(ERD)** in ion sphere by input of exterior EM wave from ground(HAARP).Collaboration by input EM and **plasma oscillation** is to generate stronger CDW toward ground.Note ERD equation at here neglects **relativity theory** and reaction force of radiation*.We assume **E** is horizontal(x axis,while **B** is y axis, of which force is perpendicular with x axis..So we neglect magnetic B for **the simplicity**(see APPENDIX6).

*Nunzio Tralli,Classical Electromagnetic Theory(McGraw-Hill),P275,1963

(0)heavy mass ions never move,but **electrons** voscillate. <displacement= $\delta x \equiv x$ >.

$$* m_e(d^2x/dt^2) = -m_e(dx/dt) \cdot N_e \sigma_I [(dx/dt) - (e^2 N_e / \epsilon) x - e E_0 \exp(j \omega t)] \dots \dots \dots \text{ERD.}$$

☞ : Note this is **non relativistic equation** which allows velocity= $\omega A > c_0$. See (6).

$|(dx/dt)|(dx/dt)$ becomes **energy loss term** attenuating input EM Wave.

$$P_L = \mathbf{f} \cdot \mathbf{V} = m_e(dx/dt) \cdot N_e \sigma_I |(dx/dt)|.$$

(1) E_p :Electric Intensity caused by charge distribution ρ in medium of ϵ (1dim model).

$$\square E = \text{grad} \rho / \epsilon. \rightarrow \partial^2 E_x / \partial x^2 = (\partial \rho / \partial x) / \epsilon. \rightarrow E_x = \epsilon^{-1} \int_0^x \rho(u) du. \rightarrow E_x = x \langle \rho \rangle / \epsilon. * <\text{average}>$$

(2) $F_c = f_c m_v$:momentum absorption force(by **averaging**)on **random** collision with ions.

Definition on **average mean path length** : $\lambda N \sigma \equiv 1. \rightarrow f_c \equiv V / \lambda = V N \sigma$.

$$f_c = |dx/dt| N_e \sigma_I. \quad N_e = \text{ion density} = \text{electron density}, \quad \sigma = \text{cross section of ion(Nitrogen),}$$

☞ : Our assumption neglect **y axis trajectory** due to magnetic field B,so f_c must be

multiply by factor $\alpha \equiv (\text{full path length/sec}) / V \sim 2?$.This could be accomplished by $\sigma_I \rightarrow \alpha \sigma_I$

$$*(3)(d^2x/dt^2) = -(N_e \sigma_I |dx/dt|)(dx/dt) - (e^2 N_e / m_e \epsilon) x - (e / m_e) E_0 \exp(j \omega t).$$

This is a **non linear equation**,so we must take something approximation method.

Author assume something constant $K \equiv |dx/dt|$ in **average meaning** of periodic solution toward final adjust. Then the equation shall become linear one with $x = A \cdot \exp(j \omega t)$.

$$-A \omega^2 = -i(N_e \sigma_I K) \omega A - (e^2 N_e / m_e \epsilon) A - (e / m_e) E_0.$$

$$A[-\omega^2 + i(N_e \sigma_I) \omega K + (e^2 N_e / m_e \epsilon)] = -(e / m_e) E_0.$$

$$A = -E_0 (e / m_e) / [(e^2 N_e / m_e \epsilon) - \omega^2 + i(N_e \sigma_I) \omega K]. \quad \text{Note A is complex,but not real.}$$

$$(4)|A| = E_0 (e / m_e) / \sqrt{[(\omega_p^2 - \omega^2)^2 + (N_e \sigma_I)^2 \omega^2 K^2]}. \quad <* \omega_p^2 \equiv (e^2 N_e / m_e \epsilon_0).>$$

$$e = 1.61 \times 10^{-19}, \quad m_e = 9.1 \times 10^{-31}, \quad \sigma_I = \sigma_N = \pi (65 \times 10^{-12} \text{m})^2 = 1.3 \times 10^{-20} \text{m}^2, \\ N_e = 10^{12} / \text{m}^3. (\text{E layer}); \quad (N_e \sigma_I) = 1.3 \times 10^{-8}. \quad (e / m_e) E_0 = 1.76 \times 10^{11} E_0. \quad \epsilon_0 = 8.85 \times 10^{-12} \text{F/m}$$

$$(5)f_p = \sqrt{(e^2 N_e / m_e \epsilon_0)} / 2 \pi = 8.97 \sqrt{N_e}.$$

(6) $K \equiv \langle |dx/dt| \rangle = \langle |j \omega A \exp(j \omega t)| \rangle = (2/\pi) \omega |A|$. **<The average velocity for collisions>**.

(7) $|A| = E_0(e/m_e) / \sqrt{[(\omega_P^2 - \omega^2)^2 + (2/\pi)^2 (N_e \sigma_I)^2 \omega^4 |A|^2]}$

$|A|^2 [(\omega_P^2 - \omega^2)^2 + (2/\pi)^2 (N_e \sigma_I)^2 \omega^4 |A|^2] = (E_0 e/m_e)^2$.

******* $(2/\pi)^2 (N_e \sigma_I)^2 \omega^4 |A|^4 + |A|^2 (\omega_P^2 - \omega^2)^2 - (E_0 e/m_e)^2 = 0$.

$|A|^2 = \{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + 4(E_0 e/m_e)^2 (2/\pi)^2 (N_e \sigma_I)^2 \omega^4]} \} / 2(2/\pi)^2 (N_e \sigma_I)^2 \omega^4$.

$4(E_0 e/m_e)^2 (2/\pi)^2 (N_e \sigma_I)^2 = (8/\pi^2) \sigma_I^2 (\epsilon_0^2 E_0^2 / e^2) (e^2 N_e / m_e \epsilon_0)^2 = (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4$.

(8) Amplitude Solution.

$|A|^2 = \{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} \} / (8/\pi^2) (N_e \sigma_I)^2 \omega^4$.

(9) **Resonance Amplitude** $\langle * \omega_P^2 = (e^2 N_e / m_e \epsilon_0) \rangle$.

$|A(\omega = \omega_P)|^2 = \sqrt{[(8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} / (8/\pi^2) (N_e \sigma_I)^2 \omega^4$

$= \sqrt{[(1/8) \pi^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} / N_e^2 \omega^4 \sigma_I$.

$|A(\omega = \omega_P)| = (1/8)^{1/4} \cdot \pi (\epsilon_0 E_0 / e) \omega_P^2 \omega^2 / N_e \omega^2 \sqrt{\sigma_I} = (1/8)^{1/4} \cdot \pi (\epsilon_0 / e) \omega_P^2 E_0 / N_e \sqrt{\sigma_I}$

$= \sqrt{\sqrt{(1/8) \pi (\epsilon_0 / e) (e^2 N_e / m_e \epsilon_0) E_0 / N_e \sqrt{\sigma_I}}} = \sqrt{\sqrt{(1/8) \pi (e/m_e) E_0 / \sqrt{\sigma_I}}}$.

*** $|A(\omega = \omega_P)| = (1/8)^{1/4} \cdot \pi (e/m_e) E_0 / \sqrt{\sigma_I}$.**

example calculation $\langle N_e = 10^{12}/m^3 \rightarrow f_P = 9\sqrt{N_e} = 9\text{MHz} \rangle$

$e = 1.6 \times 10^{-19} \text{C}; m_e = 9.1 \times 10^{-31}, \sigma_N = \pi (65 \times 10^{-12} \text{m})^2 = 1.3 \times 10^{-20} \text{m}^2$,

$* G \equiv |A(\omega = \omega_P)| / E_0 = \sqrt{\sqrt{(1/8) \pi (e/m_e) / \sqrt{\sigma_I}}}$

$= 3.3 \times 10^{11} / 1.14 \times 10^{-10} = \underline{2.9 \times 10^{21} \text{m}^2/\text{volt}}$ too large gain?! <note A is displacement in length>

example) Correction by Relativity Theory.

$E_0 = 1 \text{volt/m}, |A(\omega = \omega_P)| = \underline{2.9 \times 10^{21} \text{m}}, V = \underline{2.9 \times 10^{21} \text{m}} / (1/f_P) = \underline{2.6 \times 10^{28}} \times 3 \times 10^8 \text{m/s}$.

Yes! upper limit of A, $x = \lambda / 2 = 16.7 \text{m}$ ($f_P = 9\text{MHz}$). G is not correct.

Note: $e(e N_e / \epsilon) x \equiv e E_N \rightarrow \epsilon E_N = D_N = (e N_e) x = (e N_e) G E_0$. **Charge Alternater !!**

Electric flux D_N is **alternate surface charge density** which can re-radiate charge density wave

$= \phi$ toward ground !

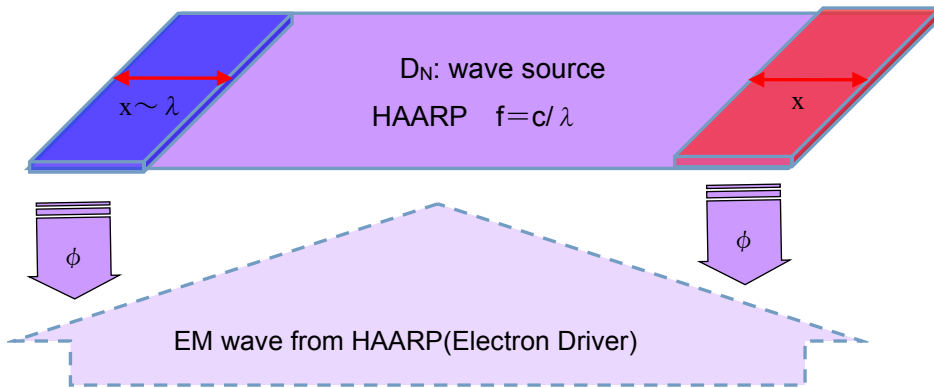
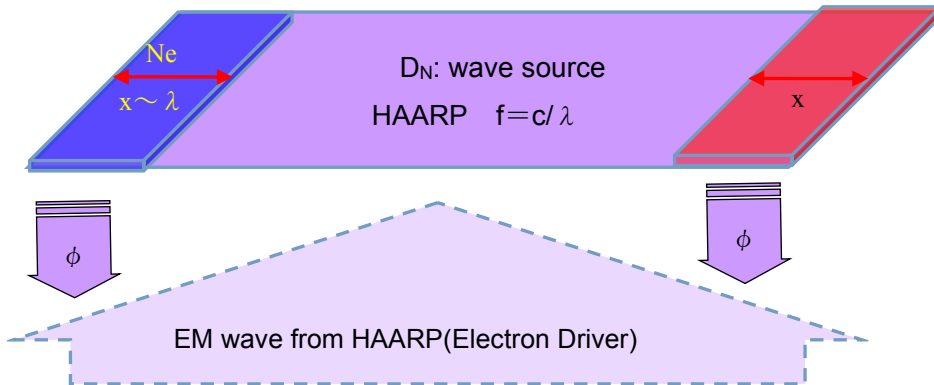
$\rightarrow \square \phi = 0; \leftarrow \phi = \oint \mathbf{S} \cdot \mathbf{D} / 4\pi \epsilon R$.

Conclusion:

Velocity of stretching A is to be over that of light, so we should assume **max A = $\lambda / 2$** in case of

resonance at $\omega = \omega_P$. Otherwise, $A < \lambda / 2$.

(10) The Horizontal Charge Density Wave Radiators in Ion Sphere.

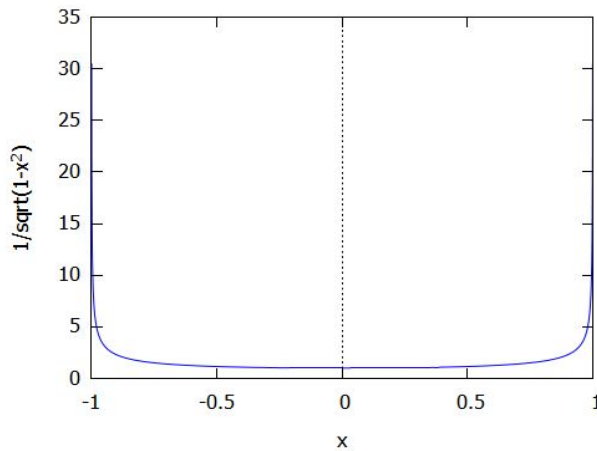


This method could not realize large area CDW antenna,so could not be HAARP.

$$x = A \sin(\omega t), t = \text{asin}(x/A) / \omega \rightarrow x = -\omega A \cos(\omega t) dt.$$

$dt/dx = -1/\omega A \cos(\omega t) = -1/\omega A \cos(\text{asin}(x/A))$ **Amplitude Density Function**

plot2d(1/cos(asin(x)), [x, -1, 1]);



APPENDIX1:

N_e	$f_p = 9\sqrt{N_e}$	$\lambda_p/2$	$G \equiv N_e \lambda_p/2$
$10^{10}/\text{cm}^3$	0.9MHz	333m	$3.3 \times 10^{12}/\text{cm}^2$
$10^{11}/\text{cm}^3$	2.8MHz	52.3m	$5.2 \times 10^{12}/\text{cm}^2$
$10^{12}/\text{cm}^3$	9MHz	16.7m	$1.6 \times 10^{13}/\text{cm}^2$
$10^{13}/\text{cm}^3$	28mHz	5.2m	$5.2 \times 10^{13}/\text{cm}^2$

APPENDIX2:

$|(dx/dt)|(dx/dt)$ becomes **energy loss term** attenuating input EM Wave in (1).

Following are energy per 1 electron,so energy volume density must multiply N_e .

$$P_L = \mathbf{f} \cdot \mathbf{V} = N_e \sigma_I m_e |(dx/dt)|(dx/dt)^2.$$

$$N_e \sigma_I m_e |(dx/dt)|(dx/dt)^2 = 10^{12} \times 10^{12} \times 3 \times 10^{-20} \times 9.1 \times 10^{-31} \times A^3/2$$

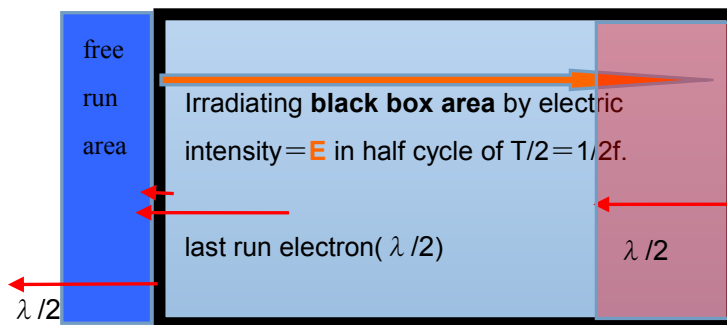
$$\sim 10^{12} \times 10^{12} \times 3 \times 10^{-20} \times 9.1 \times 10^{-31} \times \lambda^3/8.$$

This is very small ?,

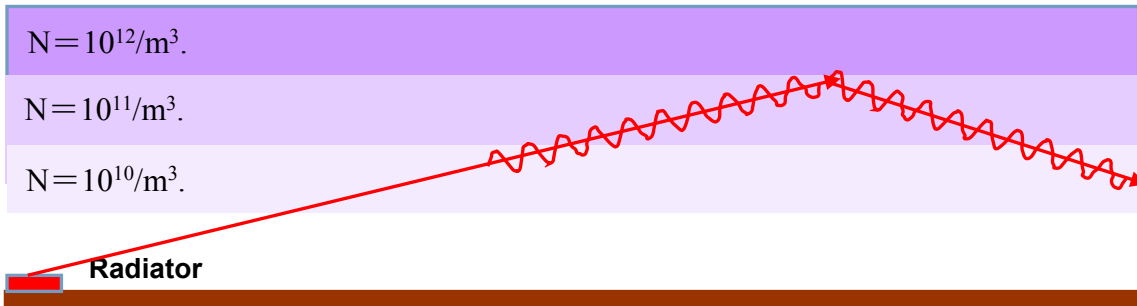
$$* \sigma_I = \sigma_N = \pi (65 \times 10^{-12} \text{m})^2 = 1.3 \times 10^{-20} \text{m}^2, N_e = 10^{12}/\text{m}^3 (\text{E layer}), m_e = 9.1 \times 10^{-31} \text{Kg}$$

$$|(dx/dt)|(dx/dt)^2 = (2/\pi) A \times A^2/2. \quad A \sim \lambda/2.$$

APPENDIX3:Un-symmetry of electron flap and ion flap.



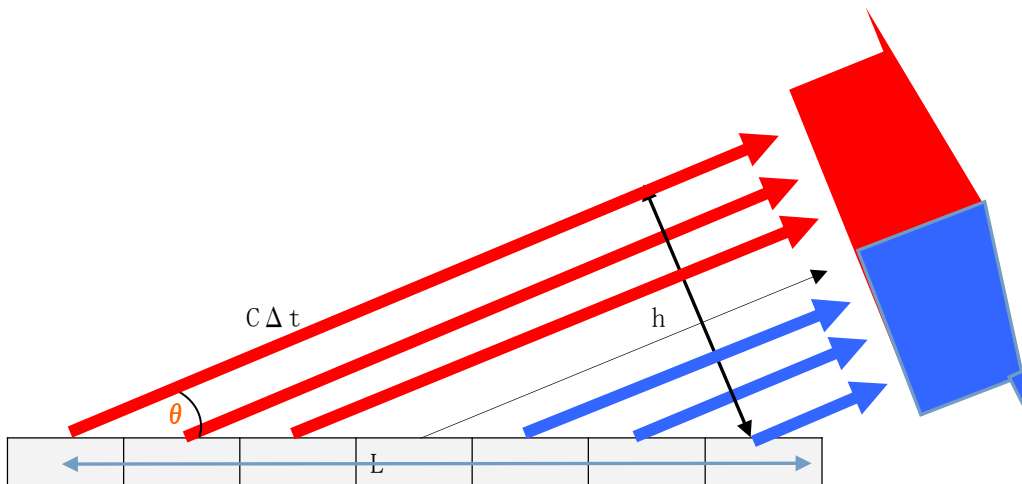
APPENDIX4:Vertical Modulation on Ion Sphere.



Vertical Modulation by Confronting Dual Electric Intensity $\pm E$.

- (1) Incident alternate EM wave irradiating ion sphere is
 - (a) Beamed plane wave with finite area of $L \times L$, where $L = n \lambda$ ($n > 10?$).
 - (b) $\lambda = c/f$: wave length.
 - (c) Electric field = E is vertical.
 - (d) Phased array radiator.

Beamed wave is enough exact to modulate ion sphere field.



$\pm E$ Dual Finite Plane Wave.

$$E_x(x;t) = E_y(x;t) = 0$$

$$E_z(x;t) = E(z) \exp(kx - \omega t)$$

$$E_z(z > 0) \doteq +E_0, \quad E_z(z < 0) \doteq -E_0.$$

$$\square \mathbf{E}(\mathbf{r};t) = 0, \quad * \square = \nabla^2 - \partial^2 / c^2 \partial t^2.$$

$$\square \mathbf{A} = 0, \quad \leftarrow \quad \mathbf{A} = \iint \langle d\mathbf{S} \times \text{curl} \mathbf{A}(\mathbf{r}'; t-R/c) \rangle / 4\pi |\mathbf{r}-\mathbf{r}'|$$

$$= \iint \langle d\mathbf{S} \times \mathbf{B}(\mathbf{r}'; t-R/c) \rangle / 4\pi |\mathbf{r}-\mathbf{r}'|.$$

(2) W Radiator with distance $= (n+1/2)\lambda$ ($n=1,2,3,\dots$) is equivalent to nothing. $\langle k = 2\pi / \lambda \rangle$

Radiation cancellation at far points is to occur by wave source configuration. This fact becomes important in synthesizing CDW radiator in ion sphere.

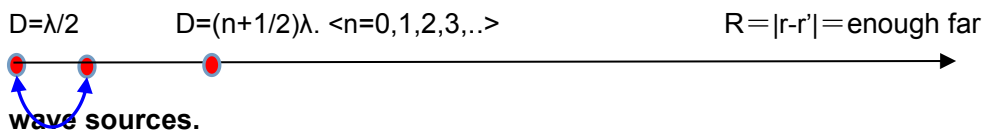
☞ : note following discussion are same phase at same time in **all wave sources**.

As would be seen in (4), that of ion sphere CDW radiator is rather different.

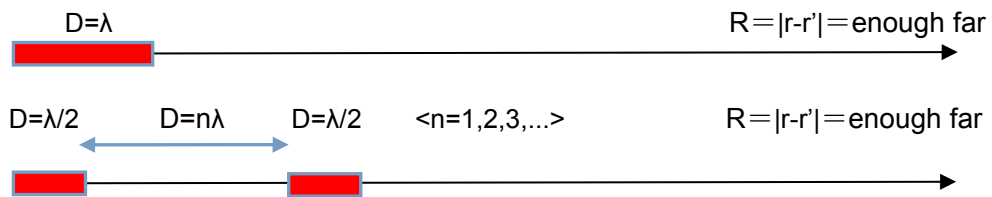
It is similar operation as opening and closing stage (**charge density stage**) curtain.

$$\phi(r,t) = \iiint dV \rho(r', t - R/c) / 4\pi\epsilon(|r-r'|) = \iiint dV \rho(r') \exp j\omega(t - R/c) / 4\pi\epsilon(|r-r'|)$$

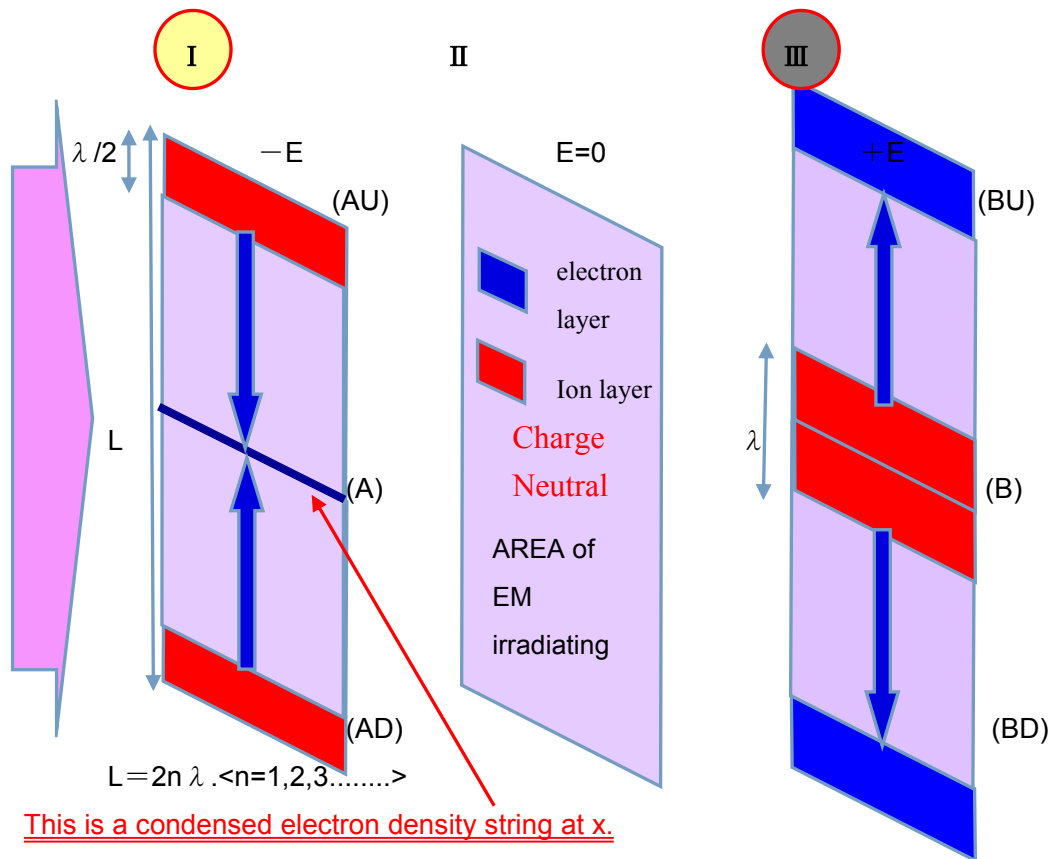
$$\exp-j(kx) + \exp-j(k(x+\lambda/2)) = \exp-j(kx) + \exp-j(kx + \pi) = 0.$$



(3) nothing radiation toward side by side line.



Pulse Trains by Flip Flop CDW Radiator



This is a condensed electron density string at x.

However as x stretching on, those becomes **charge density plane** of HAARP.

(4) By each phase of input EM, modulated electron density has also 3phase.

phase II : $E=0$ is nothing modulation. Electron and Ion density cancel with each other.

phase I : $-E$ is to collect **electron to center line (EC)**, while **ion zone** emerge at the edges by width $\lambda/2$ or less (☞:). We set irradiating height $L = n\lambda$. Thus EC and both edges become CDW radiator. Note incident EM wave is to scan x axis direction for length = U^* , which accomplish **plane wave source** (area = $L \times U$) of CDW..

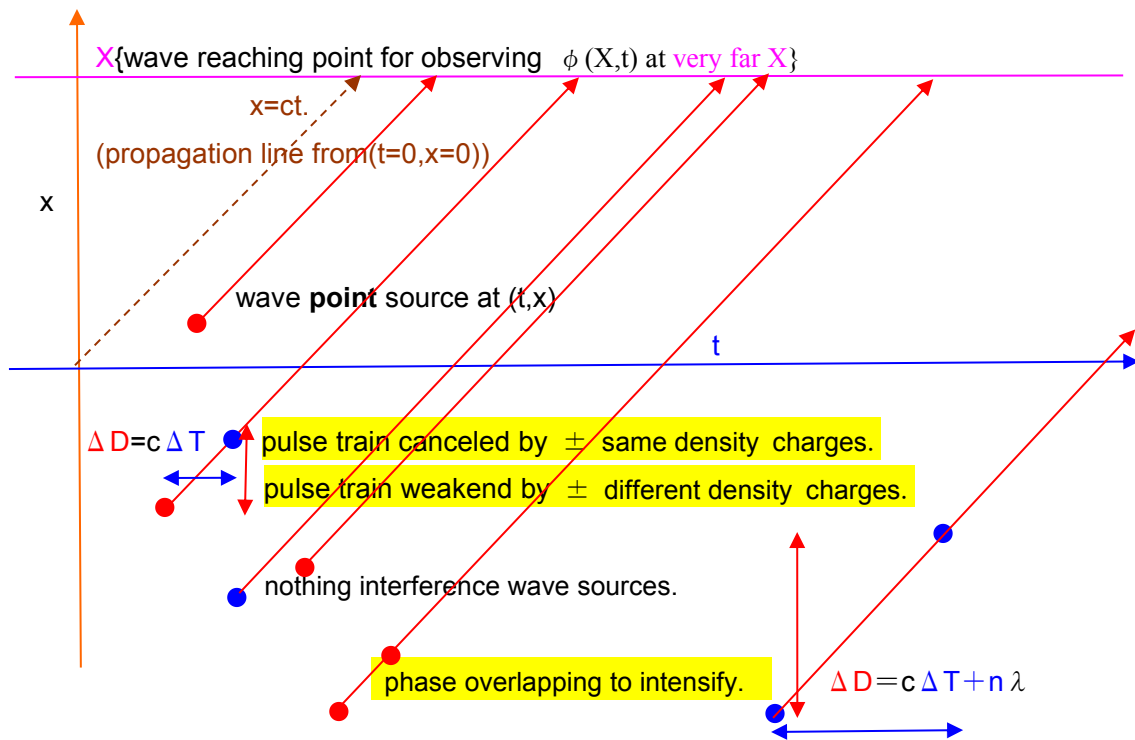
phase III : $+E$ is to emerge **ion zone at center (IC)** with width = λ , while electron zone emerge at both upper and lower edges with width = $\lambda/2$. Those also become downward radiator.

Re-radiated CDW(plane wave) is to go toward ground as alternate wave form each sources. Kernel point is that **CDW pulses trains overlapping** in **propagation space** is designed by taking **optimized sources**{A,AU,AD;B,BU,BD}**distance configuration**. Following are those discussion.

$$(5) \phi(X,t) = \int dx \rho(x,t - R/c) / 4\pi \epsilon |\mathbf{X} - \mathbf{x}|. \quad \langle R \equiv |\mathbf{X} - \mathbf{x}|, c \equiv \text{velocity of light}, K \equiv 4\pi \epsilon \rangle.$$

Retarded potential estimation is essential, note the term $t - R/c$.

In the below, we analysis **pulse train** in **propagation space** $\langle (t,x) \text{ plane from ion sphere to ground} \rangle$ from each wave source $\{A, AU, AD; B, BU, BD\}$. The problem is being of **interference between sources**. Then the condition becomes evident in below figure.

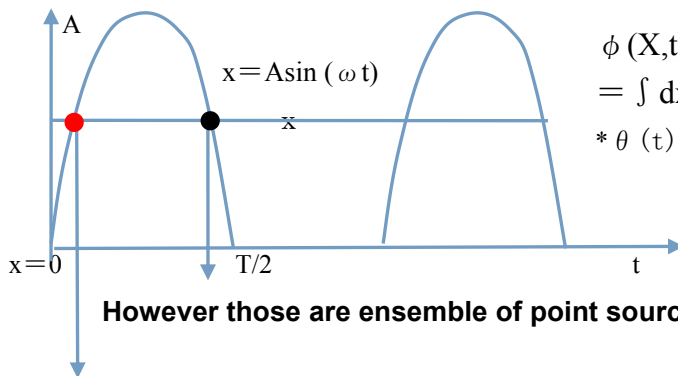


Flip Flop CDW Radiator (FFCR) are multi wave sources at different points. There by those configuration determine **interference** between those sources. **The criterion** is

$$\Delta D = c \Delta T, \text{ where } \Delta D \text{ and } \Delta T \text{ are space and time distance between two sources.}$$

Note **FFCR** sources are not point one, but **finite time and space length**.

If flip $\{AU, AD; B, BU, BD\}$ flip length are $x = A \sin(\omega t) = (\lambda/2) \sin(\omega t)$, ϕ is



$$\begin{aligned} \phi(X,t) &= \int dx \rho(x, t - |X-x|/c) / KR \\ &= \int dx \rho_0 \theta [A \sin(\omega(t - |X-x|/c))] / KR. \end{aligned}$$

* $\theta(t)$ is step function.

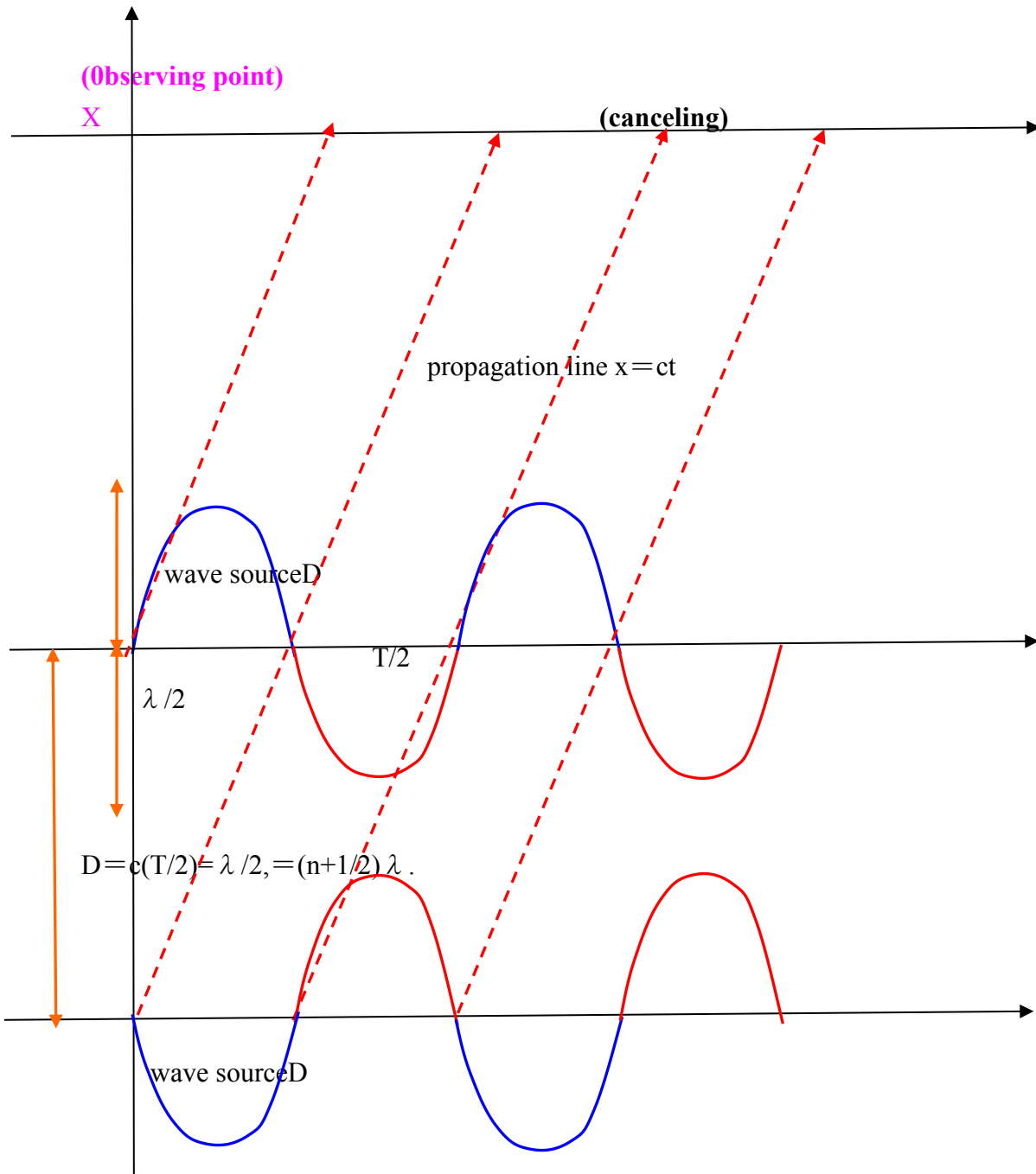
However those are ensemble of point sources expressed in above integral.

Retarded Potential as Propagating Wave Synthesizer <for example>.

$$\phi(\mathbf{X}, t) = \int dx \rho(x, t - |\mathbf{X} - \mathbf{x}|/c) / R = \int dx \rho_0 \theta [A \sin(\omega(t - |\mathbf{X} - \mathbf{x}|/c))] / R.$$

Propagator of same charge Overlapping → intensifying

Propagator of different charge Overlapping → weakening

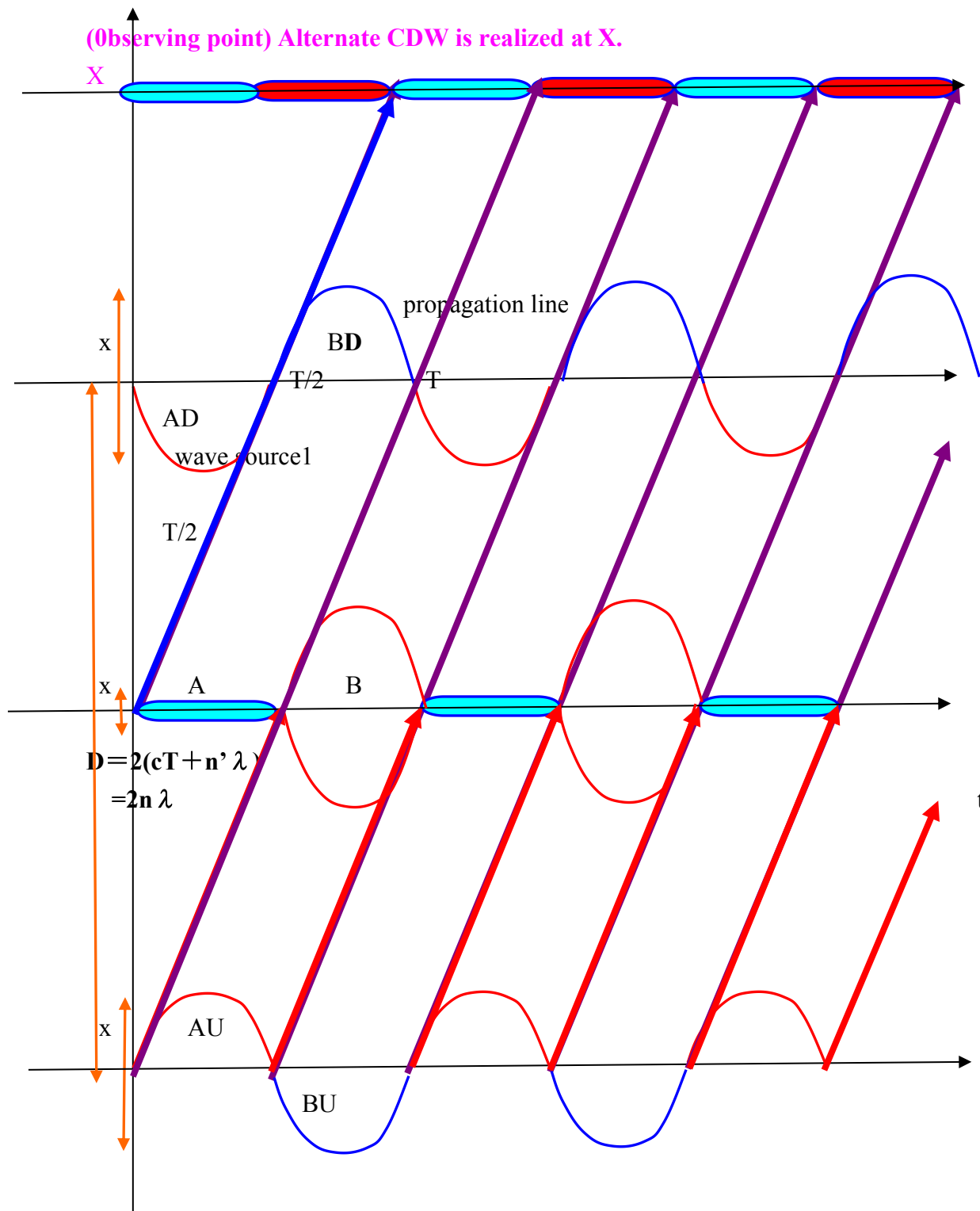


Retarded Potential as Propagating Wave Synthesizer.

$$\Phi(\mathbf{X},t) = \int dx \rho(x,t-|\mathbf{X}-x|/c)/R = \int dx \rho_0 \theta [A \sin(\omega(t-|\mathbf{X}-x|/c))]/R.$$

No Canceling between A and {AD,AU}. And overlapping between {AD and AU}.

No Canceling between B and {BD,BU}. And overlapping between {BD and BU}.



APPENDIX4:Sample calculation of A(ω).

Note this is not exact calculation due to no consideration of relativistic effect.

$$|A|^2 = \{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} / (8/\pi^2) (N_e \sigma_I)^2 \omega^4 \}$$

$$|A| = \{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} \}^{1/2} / (2\sqrt{2}/\pi) (N_e \sigma_I) \omega^2.$$

Variable{ $\omega = 2\pi \times 2.8\text{MHz} = 17.6 \times 10^6$., $\sim 2\pi \times 28\text{MHz} = 17.6 \times 10^7$.;

$$E_0 = 1 \sim 1000\text{V/m}$$

$$e = 1.61 \times 10^{-19}, m_e = 9.1 \times 10^{-31}, \sigma_I = \sigma_N = \pi (65 \times 10^{-12}\text{m})^2 = 1.3 \times 10^{-20}\text{m}^2,$$

$$N_e = 10^{12}/\text{m}^3. (\text{E layer}) \quad (N_e \sigma_I) = 1.3 \times 10^{-8}. \quad (e/m_e)E_0 = 1.76 \times 10^{11}E_0.$$

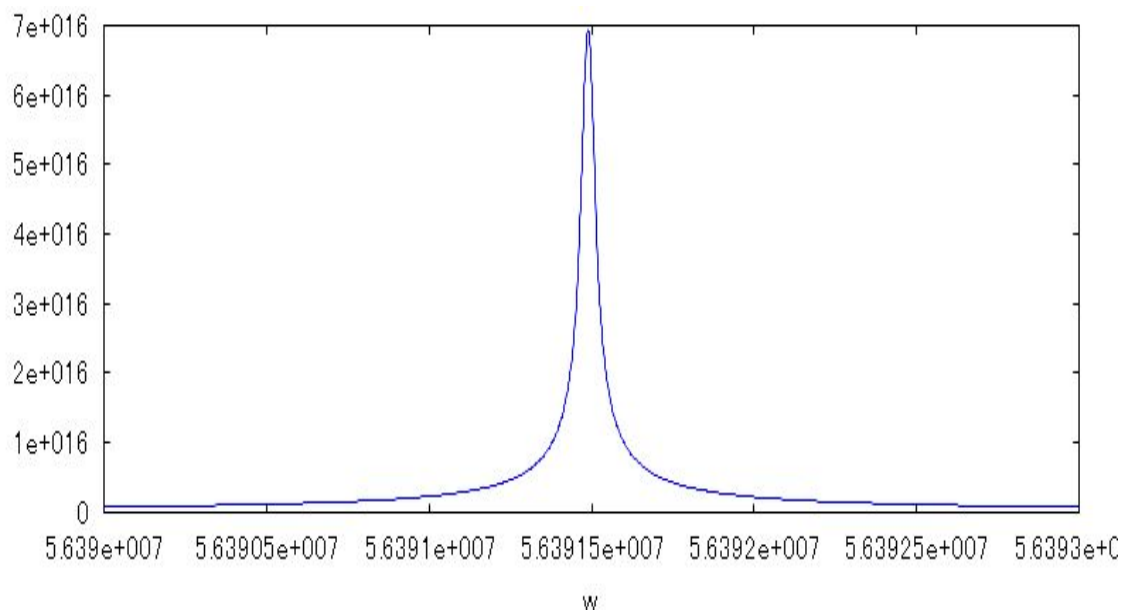
$$f_P = \sqrt{(e^2 N_e / m_e \epsilon_0)} / 2\pi = 8.97 \sqrt{N_e}. \quad \langle \epsilon_0 = 8.85 \times 10^{-12} \text{F/m} \rangle$$

$$* \omega_P = 2\pi \times 8.97\text{MHz} = 5.64 \times 10^7.$$

$$8(\sigma_I \epsilon_0 E_0 / \pi e)^2 = 4.2 \times 10^{-25}.$$

$$(2\sqrt{2}/\pi)(N_e \sigma_I) = 1.17 \times 10^{-8}.$$

plot2d((-3.18*10^15-w^2)^2+((3.18*10^15-w^2)^4+4.2*10^(-25)*10^31*w^4)^0.5)^0.5/1.17
*10^(-8)*w^2,[w,56.39*10^6,56.393*10^6]);



This is evidently too large peak value due to no consideration of relativistic effect.

Maybe electron driving force is sufficient strong to be near velocity of light.

☞ : Calculator **MAXIMA** will not reveal the tailing edges($1e+016 > 0$) .

Maybe **band width** is not so narrow.

$$|A| = \left\{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} \right\}^{1/2} / (2\sqrt{2/\pi}) (N_e \sigma_I) \omega^2.$$

Variable{ $\omega = 2\pi \times 2.8\text{MHz} = 17.6 \times 10^6$, $\sim 2\pi \times 28\text{MHz} = 17.6 \times 10^7$;

$E_0 = 1 \sim 1000\text{V/m}$ }

$$e = 1.61 \times 10^{-19}, m_e = 9.1 \times 10^{-31}, \sigma_I = \sigma_N = \pi (65 \times 10^{-12}\text{m})^2 = 1.3 \times 10^{-20}\text{m}^2,$$

$$N_e = 10^{12}/\text{m}^3 \text{ (E layer)} \quad (N_e \sigma_I) = 1.3 \times 10^{-8}. \quad (e/m_e)E_0 = 1.76 \times 10^{11}E_0.$$

$$f_P = \sqrt{(e^2 N_e / m_e \epsilon_0) / 2\pi} = 8.97 \sqrt{N_e}. \quad \langle \epsilon_0 = 8.85 \times 10^{-12}\text{F/m} \rangle$$

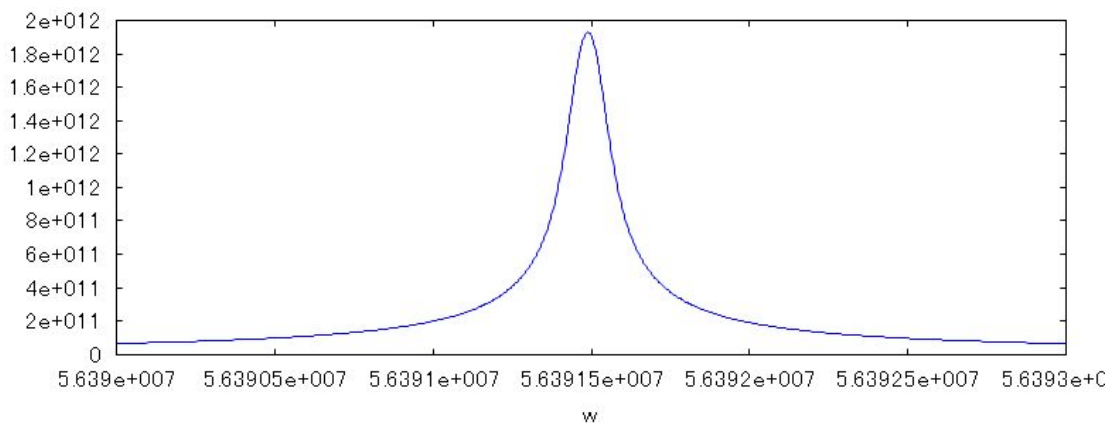
* $\omega_P = 2\pi \times 8.97\text{MHz} = 5.64 \times 10^7$.

Following are correction by increasing $\sigma_I \rightarrow 10\sigma_I$; $\rightarrow 100\sigma_I$

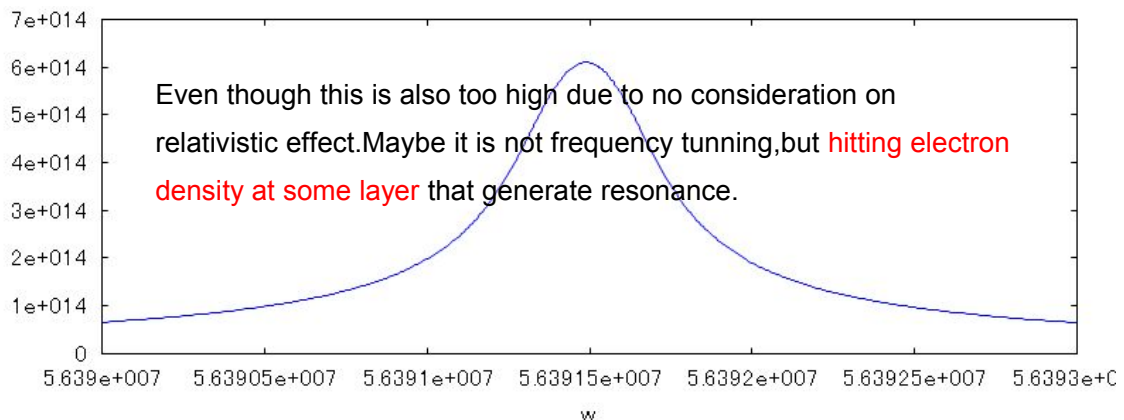
$$8(\sigma_I \epsilon_0 E_0 / \pi e)^2 = 4.2 \times 10^{-25}. \quad \rightarrow = 16.8 \times 10^{-25}.$$

$$(2\sqrt{2/\pi}) (N_e \sigma_I) = 1.17 \times 10^{-8}. \quad \rightarrow = 4.68 \times 10^{-8}.$$

plot2d((-3.18*10^15-w^2)^2+((3.18*10^15-w^2)^4+100*4.2*10^(-25)*10^31*w^4)^0.5)^0.5/
0.225*(10^12*10*1.3*10^-20)^2*w^2,[w,56.39*10^6,56.393*10^6]);



plot2d((-3.18*10^15-w^2)^2+((3.18*10^15-w^2)^4+10000*4.2*10^(-25)*10^31*w^4)^0.5)^0.5/
5/0.225*(10^12*100*1.3*10^-20)^2*w^2,[w,56.39*10^6,56.393*10^6]);



APPENDIX5: Relativistic Correction of Dynamic Equation.

Note also this is not exact calculation ,but very coarse estimation.

$$\begin{aligned}
 & m(d/dt)\langle dx/dt/\sqrt{[1-(dx/dt)^2/c^2]} \rangle \\
 & = \langle m/\sqrt{[1-\beta^2]} \rangle d^2x/dt^2 + m\beta^2 d^2x/dt^2/[1-\beta^2]^{3/2} = m\langle 1/\sqrt{[1-\beta^2]} + \beta^2/[1-\beta^2]^{3/2} \rangle d^2x/dt^2 = \\
 & = m/\sqrt{[1-\beta^2]} \langle 1 + \beta^2/[1-\beta^2] \rangle d^2x/dt^2 = m/\langle \sqrt{[1-\beta^2]} \rangle^3 d^2x/dt^2.
 \end{aligned}$$

Relativistic Correction is mass increasing by factor J (something constant in periodic motion).

$$(d^2x/dt^2) = -(N_e \sigma_I |dx/dt|)(dx/dt) - (e^2 N_e / m_e \epsilon) x - (e/m_e) E_0 \exp(j \omega t).$$

$$\rightarrow (d^2x/dt^2) = -(N_e \sigma_I |dx/dt|)(dx/dt) - (e^2 N_e / J m_e \epsilon) x - (e/J m_e) E_0 \exp(j \omega t).$$

$$= -(N_e \sigma_I |dx/dt|)(dx/dt) - (e^2 N_e / m_e \epsilon)(x/J) - (e/m_e)(E_0/J) \exp(j \omega t).$$

It may be decreasing also E_0 by (E_0/J) ..

Relativistic Correction by $E_0 \rightarrow (E_0/J)$.

$$|A| =$$

$$\{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 E_0 / e)^2 \omega_P^4 \omega^4]} \}^{1/2} / (2\sqrt{2/\pi}) (N_e \sigma_I) \omega^2.$$

↓

$$|A| =$$

$$\{ -(\omega_P^2 - \omega^2)^2 + \sqrt{[(\omega_P^2 - \omega^2)^4 + (8/\pi^2) \sigma_I^2 (\epsilon_0 (E_0/J)) / e)^2 \omega_P^4 \omega^4]} \}^{1/2} / (2\sqrt{2/\pi}) (N_e \sigma_I) \omega^2.$$

It may be decreasing peak amplitude value as $|A| \leq c/2f$.

APPENDIX6:Charge Particle Equations in Alternate EM Filed. 2016/4/26,28

(1) $d\mathbf{V}/dt = (q/m) \mathbf{E} + (q/m) \mathbf{V} \times \mathbf{B}.$

$$\mathbf{V} \times \mathbf{B} = \begin{pmatrix} \mathbf{e}_x & \mathbf{e}_y & \mathbf{e}_z \\ V_x & 0 & V_z \\ 0 & B \sin(\omega t) & 0 \end{pmatrix} \quad \begin{aligned} \mathbf{E} &= [0, 0, E \sin(\omega t)] \\ \mathbf{B} &= [0, B \sin(\omega t), 0] \\ \mathbf{V} &= [V_x, 0, V_z] \end{aligned}$$

$= [-V_z B \sin(\omega t), 0, V_x B \sin(\omega t)].$

$dV_z/dt = q E \sin(\omega t) + V_x B \sin(\omega t)$	$\rightarrow V_x = \langle (dV_z/dt) - q E \sin(\omega t) \rangle / B \sin(\omega t)$
$dV_x/dt = -V_z B \sin(\omega t)$	$\rightarrow V_z = -(dV_x/dt) / B \sin(\omega t).$

(2)method of variable separation.

$$\rightarrow dV_z^2/dt = 2dV_z/dt \cdot V_z = -2[q E \sin(\omega t) + V_x B \sin(\omega t)](dV_x/dt) / B \sin(\omega t)$$

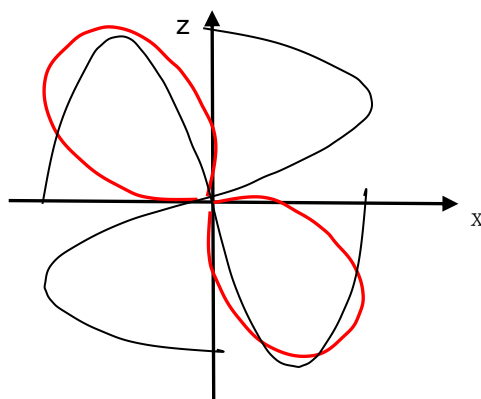
$$= (d/dt)[-dV_x/dt / B \sin(\omega t)]^2.$$

$$\rightarrow dV_x^2/dt = 2 \cdot V_x \cdot dV_x/dt = -2V_z B \sin(\omega t) \langle (dV_z/dt) - q E \sin(\omega t) \rangle / B \sin(\omega t)$$

$$= (d/dt)[\langle (dV_z/dt) - q E \sin(\omega t) \rangle / B \sin(\omega t)]^2.$$

*As are seen in this Appendix6,this report can not be complete by author, but recommend you to revise those toward completion.

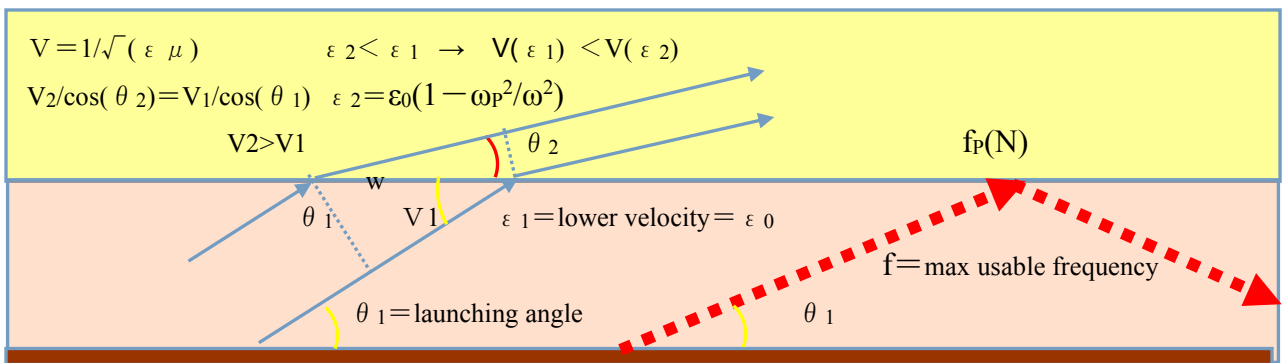
Imagined electron trajectory in cyclic mode(=W looping).



APPENDIX7:Secant Law as VHF Reflection by Ion Sphere Layer.

- (1) $\text{curl}\mathbf{H} = \partial_t\mathbf{D} + \mathbf{j} = (j\omega\epsilon_0 + (Ne^2/j\omega m))E\exp(i\omega t)$
 $= j\omega\epsilon_0(1 - Ne^2/\epsilon_0 m\omega^2)E\exp(i\omega t) \equiv j\omega E\exp(i\omega t)\epsilon_0(1 - \omega_p^2/\omega^2) \rightarrow \omega_p^2 \equiv Ne^2/\epsilon_0 m.$
 $\rightarrow \epsilon_0(1 - \omega_p^2/\omega^2) \equiv \epsilon_{01}$ <permittivity of ion sphere with density N>
- (2) $m(d\mathbf{V}/dt) = e\mathbf{E}\exp(i\omega t) \rightarrow \mathbf{V} = (e/j\omega m)E\exp(i\omega t).$
- (3) $\mathbf{j} = Ne\mathbf{V} = Ne \cdot (e/j\omega m)E\exp(i\omega t).$

(4)Inflection Law.



- (5) **Secant Law** < $\sin(\theta_1) = f_p/f$; $\omega_p^2 \equiv Ne^2/\epsilon_0 m$ >
 $w = V_2/(\cos\theta_2) = V_1/\cos(\theta_1) \rightarrow \cos(\theta_1)/(\cos\theta_2) = V_1/V_2 = \sqrt{(\epsilon_2/\epsilon_1)}$.
 $\sin(90-\theta_1)/\sin(90-\theta_2) = \cos(\theta_1)/\cos(\theta_2) = \sqrt{(\epsilon_2/\epsilon_1)} = \sqrt{(\epsilon_1/\epsilon_0)} = \sqrt{1 - Ne^2/m\epsilon_0\omega^2}$.
 $\cos(\theta_1)/(\cos\theta_2) = V_1/V_2 = \sqrt{(\epsilon_2/\epsilon_1)} \rightarrow \theta_2 = 0 \rightarrow \cos(\theta_1) = V_1/V_2 = \sqrt{(\epsilon_2/\epsilon_1)}$.
 $\cos^2(\theta_1) = (\epsilon_2/\epsilon_1) = (1 - \omega_p^2/\omega^2) = 1 - \sin^2(\theta_1) \rightarrow \sin(\theta_1) = \omega_p/\omega$.

(6)The meaning of secant law the near resonance mode.

$\omega_p < \omega \rightarrow 1 > \epsilon_2 = \epsilon_0(1 - \omega_p^2/\omega^2) = \epsilon_0 \cos^2(\theta_1) > 0.$

Thus MUF (maximum usable frequency for communication) is near resonance mode.

- (7) Incident wave with f_p can generate **full resonance** in N density layer even any launching angle $= \theta_1 < 90^\circ$, so such wave reflect and return toward ground. Such wave never fail to generate **CDW radiation** by mentioned mechanism in **APPENDIX4:(4)**.

HAARP uses plasma oscillation to gain CDW intensity !!!

Certainly ion sphere is string of **Satan's harp** radiating harmful **CDW** toward grand and stratum to generate **earthquake at critical hypo-center**.

HAARP is nothing, but unprecedented criminal against humanity.